



Coterminal angles

Answer the following.

(a) Find an angle between 0° and 360° that is coterminal with -495° .

(b) Find an angle between 0 and 2π that is coterminal with $\frac{11\pi}{2}$.

Give exact values for your answers.

Two angles are coterminal if they have the same initial and terminal sides.

For a given angle θ , adding or subtracting a complete revolution gives an angle coterminal with θ .

A complete revolution is 2π radians, which is 360° .

So, to get an angle coterminal with θ , we add or subtract a multiple of 2π or 360° .

(a) Note that -495° is between $-2 \cdot 360 = -720^\circ$ and -360° .
If we add 720° , we get a coterminal angle between 0° and 360° .

$$-495 + 720 = 225^\circ$$

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(b) Find an angle between 0 and 2π that is coterminal with $\frac{11\pi}{2}$.

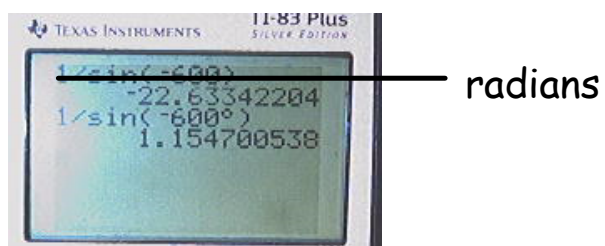
$$11\pi/2 * 180/\pi = 990$$

convert to degrees...use what you know

$$990 - 720 = 270$$

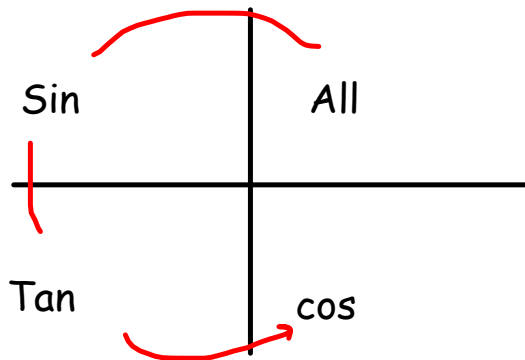
then convert back to radians

$$270 * \pi/180 = 3\pi/2$$



$$\csc\left(\frac{\pi}{3}\right) = \frac{2}{\sqrt{3}} \left(\frac{\pi}{3}\right) = 1.15\dots$$

$$\left| \csc(-600^\circ) = \frac{2\sqrt{3}}{3} \right|$$



all student take calculus

ASTC

QI: ALL trig functions +

QII: Sine is +(csc +)

QIII: Tangent is +(cot +)

QIV: Cosine is +(sec +)

Finding trigonometric ratios from a point on the unit circle

Suppose that θ is an angle in standard position whose terminal side intersects the unit circle at $\left(-\frac{20}{29}, -\frac{21}{29}\right)$.

Find the exact values of $\sin \theta$, $\tan \theta$, and $\sec \theta$.

Suppose that θ is an angle in standard position.

Let (x, y) be the terminal point of θ (where the terminal side of θ intersects the unit circle). Then the six trigonometric functions are defined as follows.

$$\sin \theta = y$$

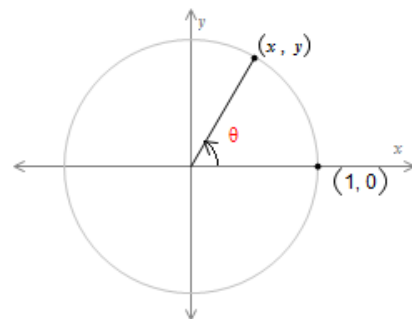
$$\csc \theta = \frac{1}{y}, \quad y \neq 0$$

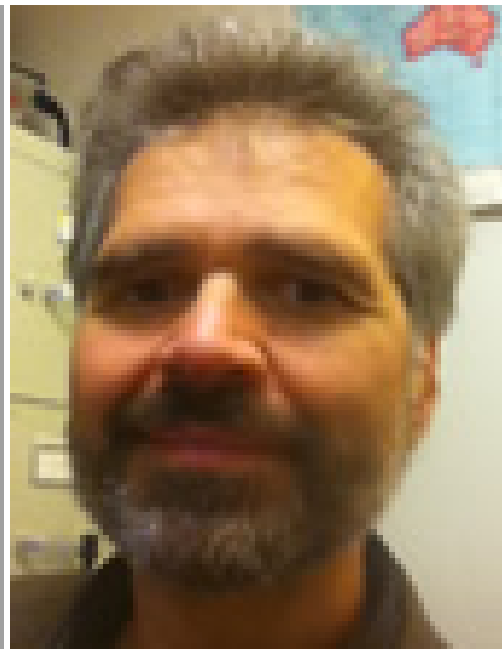
$$\cos \theta = x$$

$$\sec \theta = \frac{1}{x}, \quad x \neq 0$$

$$\tan \theta = \frac{y}{x}, \quad x \neq 0$$

$$\cot \theta = \frac{x}{y}, \quad y \neq 0$$





$$\text{EX: } \log_3(x) + \log_3(x-1) = \log_3(5)$$

Property: _____ | Prop 3: Ladder

$$\log_3(x) + \log_3(x-1) = 2 \log_3(5)$$

**Day 16:REVISED Midterm (2) - Question #1;
Polynomial long division: Problem type 1**

Divide.

$$(x^2 + 6x + 4) \div (x + 2)$$

Your answer should give the quotient and the remainder.

We can write the division like this.

$$\begin{array}{r} \\ x+2 \overline{) x^2 + 6x + 4} \end{array}$$

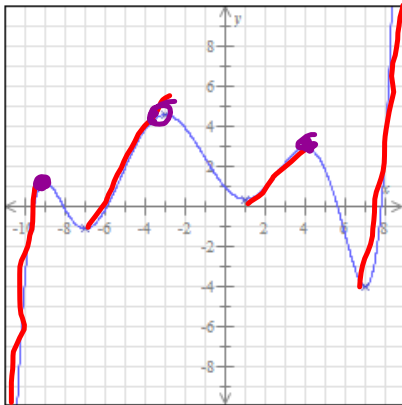
We start the division with the leading terms and get $\frac{x^2}{x} = x$.

Then, we multiply x by $x + 2$ to get $x^2 + 2x$ and subtract the result as shown below.

$$\begin{array}{r} \\ x+2 \overline{) x^2 + 6x + 4} \\ \underline{-(x^2 + 2x)} \\ 4x + 4 \\ \underline{-(4x + 8)} \\ -4 \end{array}$$

[More](#)

Quotient: $x+4$ remainder: -4



(a) The function f is increasing over which intervals? Choose all that apply.

$(-\infty, -9)$
 $(-7, -3)$
 $(1, 4)$
 $(4, 7)$
 $(1, 7)$
 $(7, \infty)$

(b) The function f has local maxima at which x -values? If there is more than one value, separate them with commas.

-9,-3,4

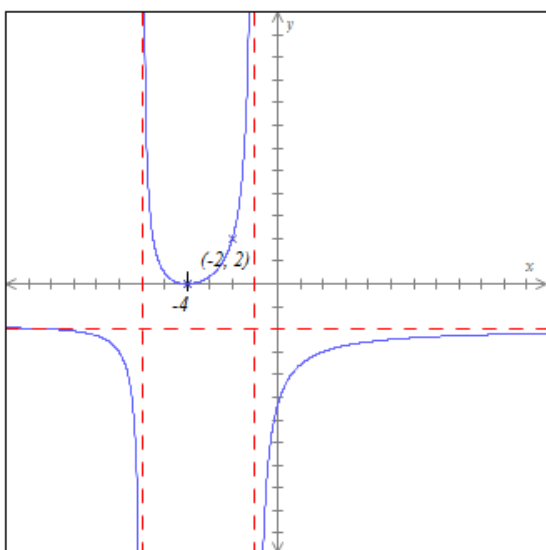
(c) What is the sign of the leading coefficient of f ?

positive because disco right

(d) Which of the following is a possibility for the degree of f ? Choose all that apply.

4
 5
 6
 7
 8
 9

because disco = odd degree, 7 faces means no 5,3,1



- $f(x) = \frac{a}{x - b}$
- $f(x) = \frac{a(x - b)}{x - c}$
- $f(x) = \frac{a}{(x - b)(x - c)}$
- $f(x) = \frac{a(x - b)}{(x - c)(x - d)}$
- $f(x) = \frac{a(x - b)(x - c)}{(x - d)(x - e)}$

$$a = -2$$

ALEKS: Prof. Porter - Windows Internet Explorer

SMART Ink

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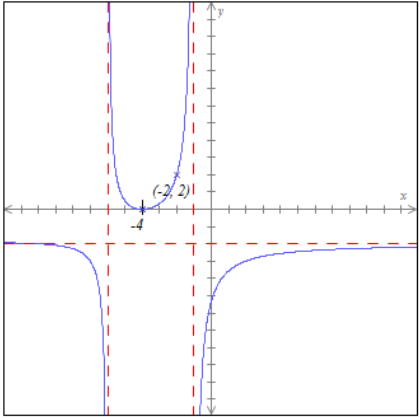
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Day 16:REVISED Midterm (2) - Question #3;
Writing the equation of a rational function given its graph

The figure below shows the graph of a rational function f with vertical asymptotes $x = -1$, $x = -6$, and horizontal asymptote $y = -2$. The graph also has an **x-intercept of -4** and it passes through the point $(-2, 2)$.

touches means zero repeated twice!

The equation for $f(x)$ has one of the five forms shown below. Choose the appropriate form for $f(x)$, and then write the equation. You can assume that $f(x)$ is in simplest form.



- $f(x) = \frac{a}{x - b}$
- $f(x) = \frac{a(x - b)}{x - c}$
- $f(x) = \frac{a}{(x - b)(x - c)}$
- $f(x) = \frac{a(x - b)}{(x - c)(x - d)}$
- $f(x) = \frac{a(x - b)(x - c)}{(x - d)(x - e)}$

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zeros: $-4, -4$

$$y = \frac{a(x+4)(x+4)}{(x+6)(x+1)} \quad \text{to find } a: \text{ plug in point } (-2, 2)$$

VA: $-6, -1$

$$2 = \frac{a(2)(2)}{4 \cdot -1} \quad a = -2$$

ORRRRRR

$a = -2$ because..

HA: $y = -2$

The mass of a radioactive substance follows a *continuous exponential decay model*, with a decay rate parameter of 5.7% per day. Find the half-life of this substance (that is, the time it takes for one-half the original amount in a given sample of this substance to decay).

Note: This is a *continuous* exponential decay model.

$$P = Qe^{rt}$$

$$r = -5.7\% = -5.7/100 = -.057$$

Math 0:solver

$$Q = 100$$

$$0 = P - Qe^{(rT)}$$

$$P = 50$$

$$r = -.057$$

$$T = \text{guess}$$

$$T = 12.16 \text{..days}$$

alpha enter

Solve for x .

$$3\ln(x+2) = 12$$

by solver

math 0: solver

$$0 = 3\ln(x+2) - 12$$

$$x = \text{guess}(5)$$

$$x = 52.59\dots$$

by intersection

$$x_{\max}: 60$$

$$y_1 = 3\ln(x+2)$$

$$y_2 = 12$$

calc 5: intersect

$$x = 52.59\dots$$

by hand....

divide by 3

$$\ln(x+2) = 4$$

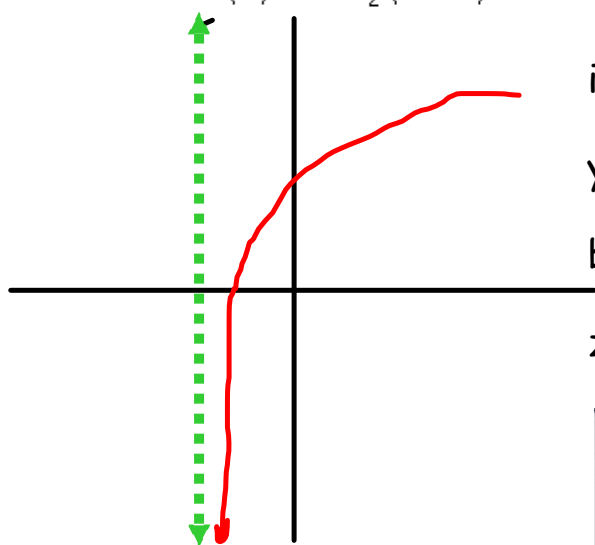
get rid of the ln

property 1:

$$e^4 = x+2$$

$$x = e^4 - 2 = 52.59\dots$$

Graph the function $g(x) = \log_2(x+1) + 3$ and give its domain and range using interval notation.

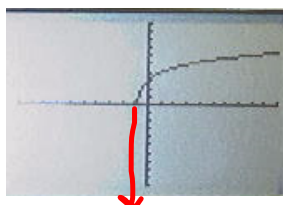


in calculator:

$$y1 = \log(x+1)/\log(2) + 3$$

by prop 4 the change of base

zoom 6:zoomstd



domain: $(-1, \infty)$

Range: all real