

Calculus: The study of change!

MV Calculus: the study of change in Multiple dimensions.

What is changing? Functions in multiple dimensions.

$f(x,y)$ Area(length,width) = $l \cdot w$

domain, range, etc.

1.

award:
10.00
points

Problems? [Adjust credit](#) for all students.

Select the domain of the given function.

$$f(x, y) = \frac{17x}{y - x^2}$$

- A. Domain = $\{(x, y) | y \neq x^2\}$
- B. Domain = $\{(x, y) | y \neq 2x\}$
- C. Domain = $\{(x, y) | y > x^2\}$
- D. Domain = $\{(x, y) | y \neq x\}$

$$y - x^2 \neq 0$$
$$y \neq x^2$$

2.

award:
10.00
pointsProblems? [Adjust credit](#) for all students.

1 out of 3 attempts

Select the domain of the given function.

$$f(x, y, z) = \frac{5xy}{\sqrt{15 - x^2 - y^2 - z^2}}$$

- A. Domain = $\{(x, y, z) \mid x^2 + y^2 + z^2 \neq 15\}$
- B. Domain = $\{(x, y, z) \mid x^2 + y^2 + z^2 > 15\}$
- C. Domain = $\{(x, y, z) \mid x^2 + y^2 + z^2 \neq 15\}$
- D. Domain = $\{(x, y, z) \mid x^2 + y^2 + z^2 < 15\}$

 $(15, 0, 0)$

gives "0" in denom.

$$15 - x^2 - y^2 - z^2 \geq 0$$

$$15 \geq x^2 + y^2 + z^2$$

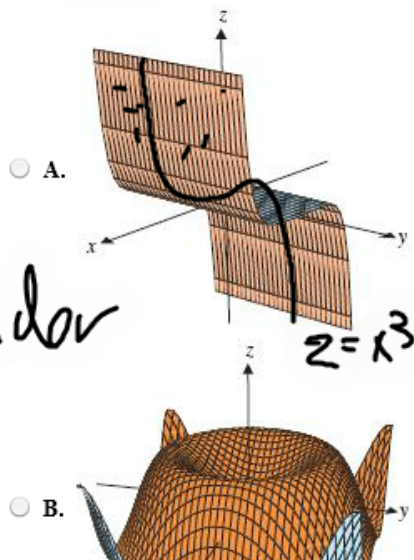


4.

award:
10.00
pointsProblems? [Adjust credit](#) for all students.

1 out of 3 attempts

$z = x^2 + 3x^3$ to the surface.



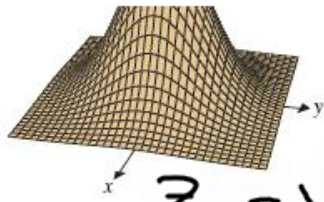
Cylinder

Graph =
collection
of points

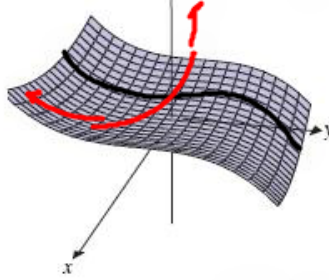
Makes

 $z = x^3$ True. $(1, 0, 1)$ $(1, 2, 1)$ $(1, 3, 1)$ [references](#)

1 out of 3 attempts

 B.

$$z = y^3$$

 C.

$$z = x^2$$

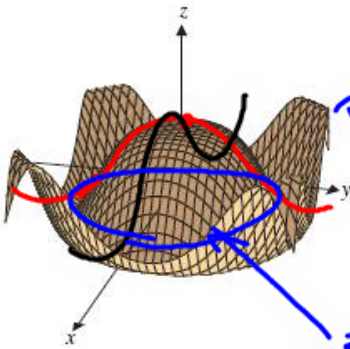


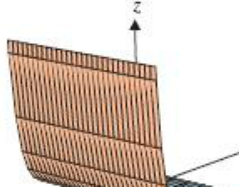
$$z = x^2 - y^3$$




1 out of 3 attempts

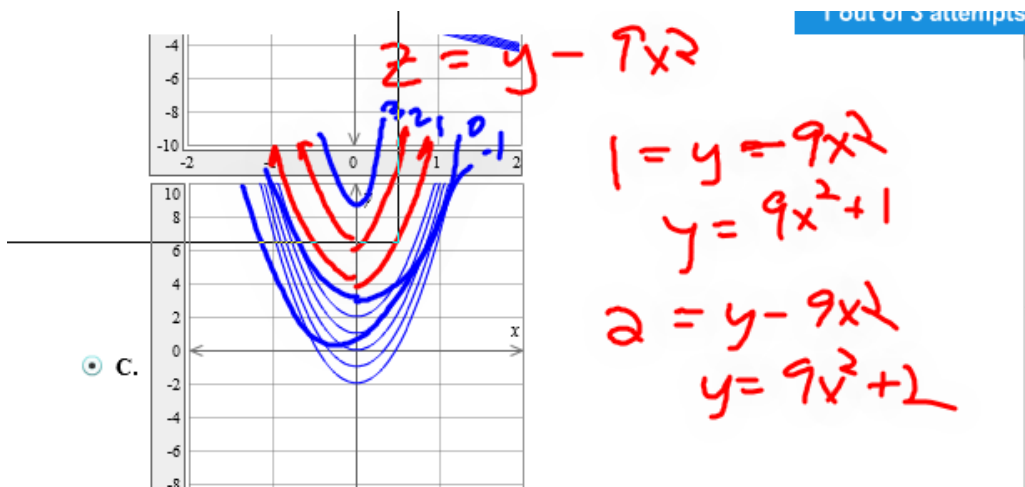
Match $f(x, y) = 3 \cos(x^2 + y^2)$ to the surface.

A. 

B. 

$x^2 + y^2 = \pi$
 $\cos(x^2 + y^2) = \cos \pi = -1$





points

1 out of 3 attempts

Evaluate $\lim_{(x,y) \rightarrow (7,0)} \frac{y}{x+y-7}$.

- A. Limit does not exist.
- B. 13
- C. 7
- D. 0

NetCalculator

Assistance

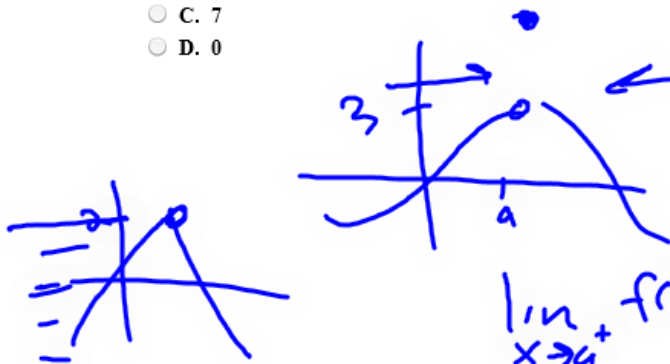
- Check My Work
- View Hint
- View Question
- Show Me
- Guided Solution
- Practice This Question
- Print
- Question Help
- Report a Problem

Path $x=7$

$$\lim_{y \rightarrow 0} \frac{y}{y} = 1$$

Path $y=0$

$$\lim_{x \rightarrow 7} \frac{0}{x-7} = 0$$



$$\lim_{x \rightarrow a^+} f(x) = \lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a} f(x)$$

TWO WAYS $\lim_{x \rightarrow 7} f(x) = 3$

True or false?

$f(x, y) = 9e^{x^4y}$ is continuous.

Notice that $f(x, y) = g(h(x, y))$, where $g(t) = 9e^t$ and $h(x, y) = x^4y$. Since g is continuous for all values of t and h is a polynomial in x and y (and hence continuous for all x and y), it follows that f is continuous for all x and y .

Thus, the statement is true.

Continuity!

Lim Exist
Function Exist
Lim = Function

prev

Question #11 (of 16)

next

11. award: 10.00 points

Problems? [Adjust credit](#) for all students.

$w = f(x, y, z)$

Evaluate $\lim_{(x, y, z) \rightarrow (0, 0, 0)} \frac{x^5 + y^5 + z^5}{x^5 + y^5 - z^5}$

- A. $\lim_{(x, y, z) \rightarrow (0, 0, 0)} \frac{x^5 + y^5 + z^5}{x^5 + y^5 - z^5} = -1$
- B. $\lim_{(x, y, z) \rightarrow (0, 0, 0)} \frac{x^5 + y^5 + z^5}{x^5 + y^5 - z^5} = 0$
- C. $\lim_{(x, y, z) \rightarrow (0, 0, 0)} \frac{x^5 + y^5 + z^5}{x^5 + y^5 - z^5} = 1$
- D. The limit does not exist.

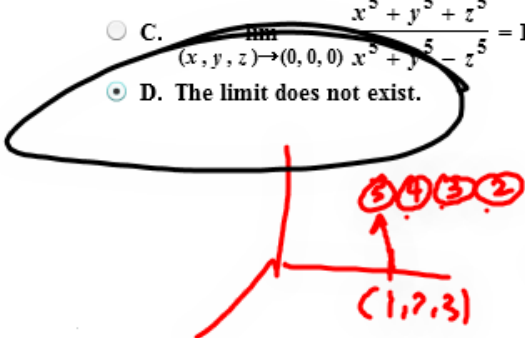
1 out of 3 attempts

$z = 0$
 $\lim f(x, y, z) = 1$

$x + y = 0$

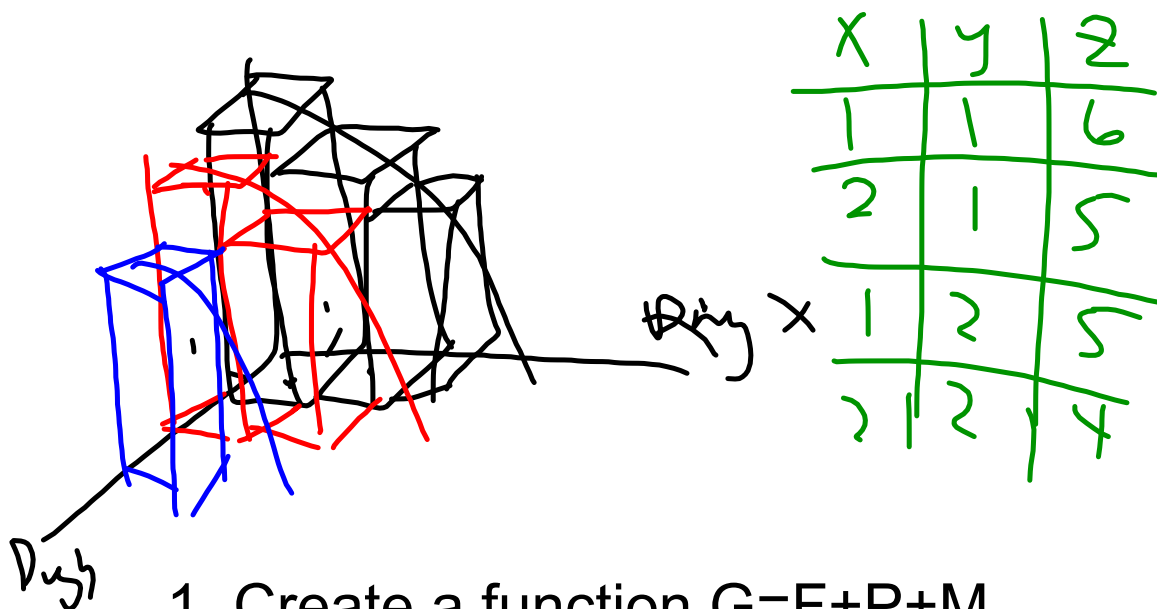
$\lim f(x, y, z) =$

$\frac{x^5 - x^5 + z^5}{y^5 - x^5 - z^5} = -1$



$f(1, 2, 3) = 5$

Create a multivariable function!



1. Create a function $G = F + P + M$

2. Write a limit

3. Write in words $(F, P, M) \rightarrow (\tilde{F}, 0, 0)$

$\lim G = \tilde{F} + 0 + 0 = \tilde{F}$

As P & M go to 0, and F goes to \tilde{F} ,
Grade becomes \tilde{F}

Independent Variable (x-axis): _____	Leader/Collaborator: Jason D.
Dependant Variable (y-axis): _____	
Conclusion (in words): At 0°W, 0°N at Midnight, the elevation of the sea compared to sea level is .042 feet.	
for Petroleum Engineering	
Supporting Work:	
The Elevation of the sea as a function of latitude, longitude, and time (in feet).	
$\xi = f(x, y, t) = \frac{\cos(t)}{x^2 + y^2 + 24}$	
$\text{At } (x, y, t) = (0, 0, 0) \quad \frac{\cos(0)}{0^2 + 0^2 + 24} = \frac{1}{24} \text{ feet}$	

As resistivity and length of a wire go to zero, the resistance of a wire becomes zero. As its area gets closer to zero, the resistance is infinite, limit DNE.

Supporting Work:

$$R = \frac{\rho L}{A}$$

ρ = resistivity

L = length

A = cross sectional area

$$\lim_{A \rightarrow 0} R(\rho, L, A) = \text{DNE}$$

Supporting Work:

$$L_F = L_i + \frac{PL}{AE}$$

$$\lim_{\substack{P \rightarrow \text{SKIPS} \\ \Delta T \rightarrow 10^\circ\text{C}}} L_F(L_i, P, A, E) = 2.5 \text{ m}$$

$$(L_i, P, A, E) = (2.53 \text{ m})$$

$$L_F = L_i + \frac{4PL}{\pi d^2 E} + L_i \alpha (\Delta T)$$

$$\lim_{\substack{P \rightarrow \text{SKIPS} \\ \Delta T \rightarrow 10^\circ\text{C}}} L_F = L_i + \frac{4PL}{\pi d^2 E} + L_i \alpha (\Delta T)$$

AS LOAD APPROACHES SKIPS
AS CHANGE IN TEMPERATURE APPROACHES 10°C

THE FINAL LENGTH IN A METAL MATERIAL IS THE
INITIAL LENGTH PLUS THE BEARING LOAD PER YOUNG'S MODULUS TIMES
THE CROSS-SECTIONAL AREA PLUS THE INITIAL LENGTH
MULTIPLIED BY THE LINEAR EXPANSION COEFFICIENT
MULTIPLIED BY THE CHANGE IN TEMPERATURE

★ THE FINAL LENGTH OF A METAL IS DETERMINED BY
★ THE INITIAL LENGTH TO THE ELONGATION DUE TO LOAD PLUS
★ THE ELONGATION DUE TO THE CHANGE IN TEMPERATURE

Supporting Work:

How quickly a server serves a web page

- Number of requests x (simultaneous)
- Temperature of server room y Celsius
- Distance between server and requester z (km)
- Server internet speeds w (gbps)
- Specs of server v (on scale of 1 to 73)

$$f(x, y, z, w, v) = \frac{w \cdot v}{x \cdot y \cdot z}$$

$$\lim_{(x, y, z, w, v) \rightarrow (100, 40, 1000, 12, 41)} f(x, y, z, w, v) = 1.23 \times 10^{-4} \frac{\text{gbps}}{\text{Celsius} \cdot \text{km}}$$

Supporting Work:

Function: $x^2 + y^2 + z^2$; $f \rightarrow$ depend on the size of the wall
Use r to calculate the size of the wall

$$\lim_{x,y,z \rightarrow (0,0,0)} f(x,y,z) = 0$$

$x, y, z \rightarrow$ points (a, a, a)



$$\lim_{(x,y,z) \rightarrow (0,0,0)} f(x,y,z) = x^2 + y^2 + z^2 = 0$$

Can be used for different sized ball bearings in Engineering.

Supporting Work:

$$\text{gas mileage} = (\text{velocity})(\text{speed})$$

$$\lim_{(M, S, A) \rightarrow 0} \frac{(A)}{(M)(S)}$$

As gas mileage goes to zero, A_0 goes to infinity