

Evaluate $\int \frac{\sin x}{3\sqrt{\cos x}} dx$.

$$\int \frac{\sin x}{3\sqrt{\cos x}} dx = \boxed{} + c$$

$$u = \cos x$$

$$du = -\sin x dx$$

$$\int \frac{-du}{3\sqrt{u}} = \frac{-1}{3} \int u^{-1/2} du$$

$$= -\frac{1}{3} \frac{u^{1/2}}{1/2} + c$$

$$= -\frac{2}{3} (\cos x)^{1/2} + c$$

Round your answer to the nearest whole number.

Compute the average value of the function $f(x) = x^2 - 5$ on the interval $[0, 3]$.

$$A = \frac{\int_0^3 x^2 - 5 dx}{3 - 0}$$

$$= \frac{\left. \frac{x^3}{3} - 5x \right|_0^3}{3 - 0}$$

$$= \frac{\left(\frac{27}{3} - 15 \right) - 0}{3 - 0}$$

$$= \frac{-6}{3} = -2$$

$$f_{\text{int}}(x^2 - 5, x, 0, 3) / (3 - 0)$$

For $f(x) = \int_2^x (t^2 - 4t + 5) dt$, compute $f'(x)$.

↓ FTC

$$F(x) = F(x) - F(2)$$

$$f'(x) = F'(x) \quad \downarrow 0$$

$$= x^2 - 4x + 5$$

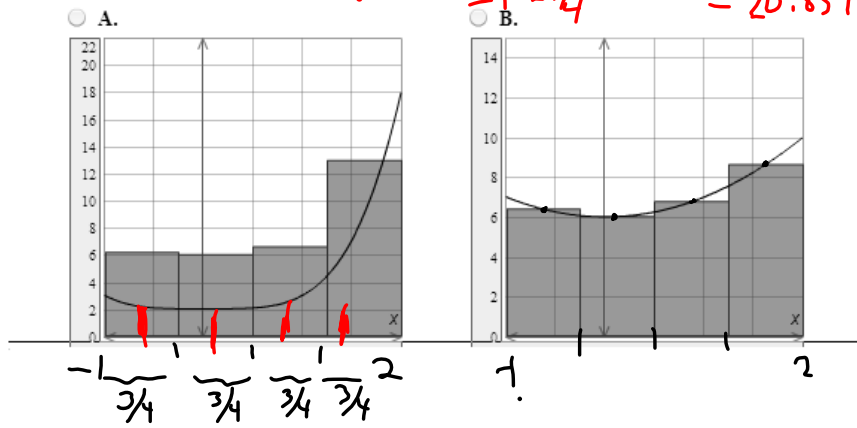
List the evaluation points corresponding to the midpoint of each subinterval to three decimal places, sketch the function and approximating rectangles and evaluate the Riemann sum to six decimal places if needed.

$f(x) = x^2 + 6$, $[-1, 2]$, $n = 4$.

Give your answer in an ascending order.

Evaluation points: $-\frac{5}{8}$, $\frac{1}{8}$, $\frac{7}{8}$ and $\frac{13}{8}$.

Sum using $(x^2+6, x_i = 5/8, 13/8, 3/4)$
 $= 20.859375$
 $* 3/4$



$-\frac{5}{8} + \frac{3}{4}$ $\frac{1}{8} + \frac{3}{4}$ $\frac{7}{8} + \frac{3}{4}$
 $-1 + \frac{3}{8}$ $\frac{1}{8}$ $\frac{7}{8}$ $\frac{13}{8}$

Compute $\int_1^9 \left(\sqrt{x} - \frac{1}{x^2} \right) dx.$

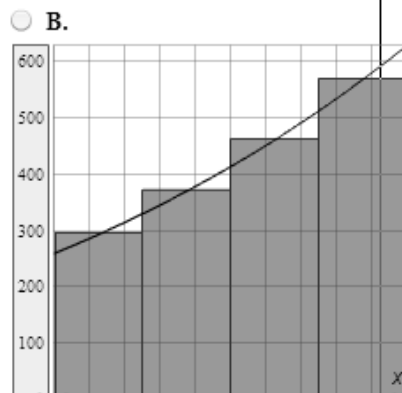
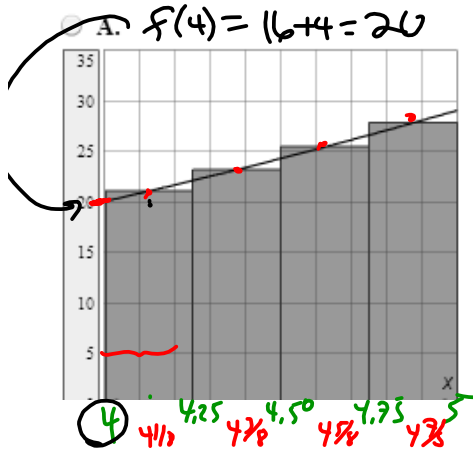
$$\begin{aligned}
 & x^{1/2} - x^{-2} \\
 & \left. \frac{x^{3/2}}{3/2} - \frac{x^{-1}}{-1} \right|_1^9 \\
 & \left(\frac{9^{3/2}}{3/2} - \frac{9^{-1}}{-1} \right) - \left(\frac{1}{3/2} - \frac{1}{-1} \right) \\
 & \frac{2}{3} \cdot \frac{27}{1} + \frac{1}{9} - \frac{2}{3} - 1 \\
 & 18 + \frac{1}{9} - \frac{2}{3} - 1 \\
 & 16 \frac{4}{9}
 \end{aligned}$$

List the evaluation points corresponding to the midpoint of each subinterval to three decimal places, sketch the function and approximating rectangles and evaluate the Riemann sum to six decimal places if needed.

$f(x) = x^2 + 4, \quad [4, 5], \quad n = 4.$

Give your answer in an ascending order.

Evaluation points: , , and .

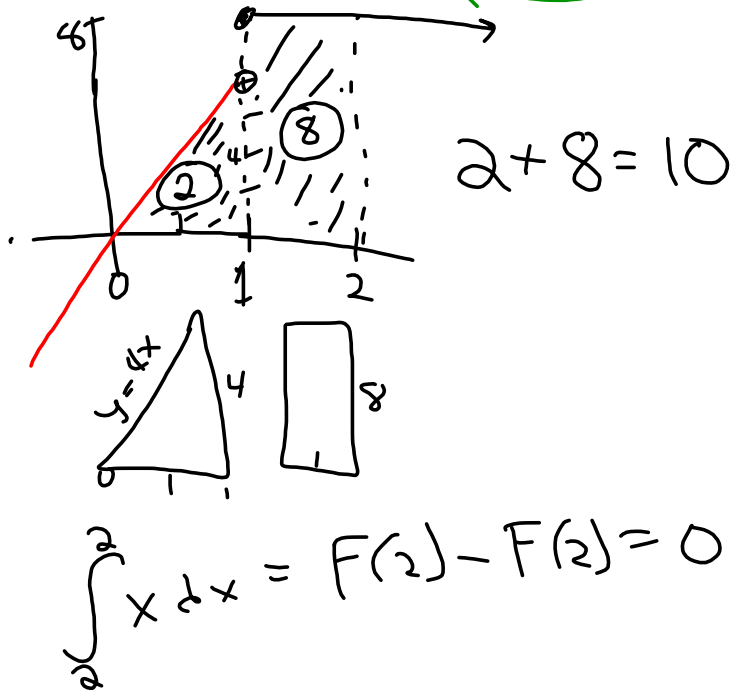


$\text{sum}(\text{seq}(x^2 + 4, x, 4.125, 5, .25)) * .25$
 $= 16.328125$

Question

Write your answer in decimal form.

Compute the area of $\int_0^2 f(x) dx$ for $f(x) = 4x$ if $x < 1$, and $f(x) = 8$ if $x \geq 1$.



Make the indicated substitution for an unspecified function $f(x)$.

$u = \sin x$ for $\int_0^{\pi/2} 2(\cos x)f(\sin x) dx$

- A. $\int_0^1 2f(u) du$
 - B. $\int_0^{1/2} f(u) du$
 - C. $\int_0^{1/2} 2f(u) du$
 - D. $\int_0^1 f(u) du$
- Handwritten notes for the substitution:
- $u = \sin x$
 - $du = \cos x dx$
 - $1 = \sin(\pi/2)$
 - $u = 0 = \sin(0)$
 - The integral is transformed to $\int_0^1 2f(u) du$
- Additional handwritten notes for option D:
- $u(\pi/2) = 1$
 - $u(0) = 0$

Use summation rules to compute the sum.

$$\sum_{i=1}^{68} (2i - 9) = \boxed{}$$

$$2 \sum_{i=1}^{68} i - 9 \sum_{i=1}^{68} 1$$

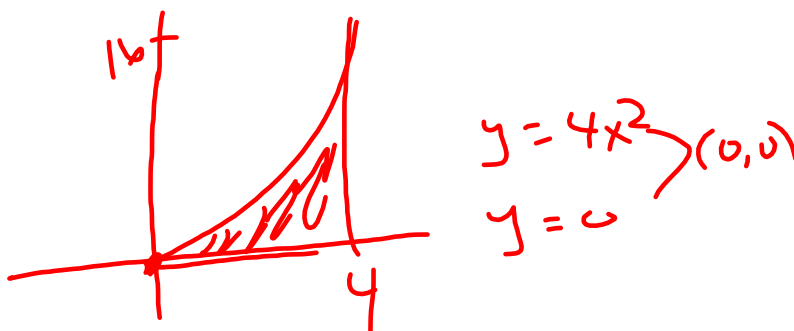
$$2 \cdot \frac{68 \cdot (69)}{2} - 9 \cdot (68)$$

$$60 \cdot \frac{68}{6} \quad \text{sum}(\text{seq}(2x-9, x, 1, 68, 1))$$

$$4080$$

Find the area of the region bounded by $y = 4x^2$, $x = 4$, and the x -axis. Express your answer as a decimal rounded to three places, if necessary.

Your Answer:



$$\int_0^4 4x^2 dx$$

Use Part I of the Fundamental Theorem to compute the integral exactly.

$$\int_0^4 x(x-4) dx$$

$$\begin{aligned} & \int x^2 - 4x dx \\ & \left. \frac{x^3}{3} - \frac{4x^2}{2} \right|_0^4 \\ & = \frac{4^3}{3} - \frac{4 \cdot 4^2}{2} \end{aligned}$$

Evaluate the given integral.

$$\int_{-80}^{80} x e^{-7x^2} dx = \int e^u \frac{du}{-14}$$

$u = -7(80)^2 = -7(80)^2$

Your Answer:

0

$$\begin{aligned} u &= -7x^2 \\ du &= -14x dx \end{aligned}$$

$$\int_a^a ? = 0$$

Find the position function $s(t)$ given the acceleration function and an initial value.

$$a(t) = 4 - t, \quad v(0) = 7, \quad s(0) = 0$$

$$a(t) = 4 - t$$

$$v(t) = \int (4 - t) dt$$

$$v(t) = 4t - \frac{t^2}{2} + C$$

$$v(0) = 7 = 0 - 0 + C \quad C = 7$$

$$v(t) = 4t - \frac{t^2}{2} + 7$$

$$s(t) = 2t^2 - \frac{t^3}{6} + 7t + C$$

$$s(0) = 0 - 0 - 0 + C = 0 \quad C = 0$$

Evaluate $\int_2^3 x^2 \sqrt{x^3 + 6} dx$.

A. $\left(\frac{1}{3}\right)\left(\frac{2}{3}\right)[14^{3/2} - 33^{3/2}]$

B. $\left(\frac{1}{3}\right)[33^{3/2} - 14^{3/2}]$

C. $\left(\frac{2}{3}\right)[33^{3/2} - 14^{3/2}]$

D. $\left(\frac{1}{3}\right)\left(\frac{2}{3}\right)[33^{3/2} - 14^{3/2}]$

$$u = x^3 + 6$$

$$du = 3x^2 dx$$

$$\frac{du}{3} = x^2 dx$$

$$\int_{14}^{33} \sqrt{u} \left(\frac{du}{3}\right)$$

$$\left(\frac{1}{3}\right) \frac{u^{3/2}}{3/2} \Big|_{14}^{33}$$

$$\left(\frac{2}{3}\right)\left(\frac{1}{3}\right) \left((33)^{3/2} - (14)^{3/2} \right)$$

