

2.4
#2

HW #4

$$2. \quad 0 < |x-5| < \delta \quad \cdot \quad |f(x)-3| < 0.6$$

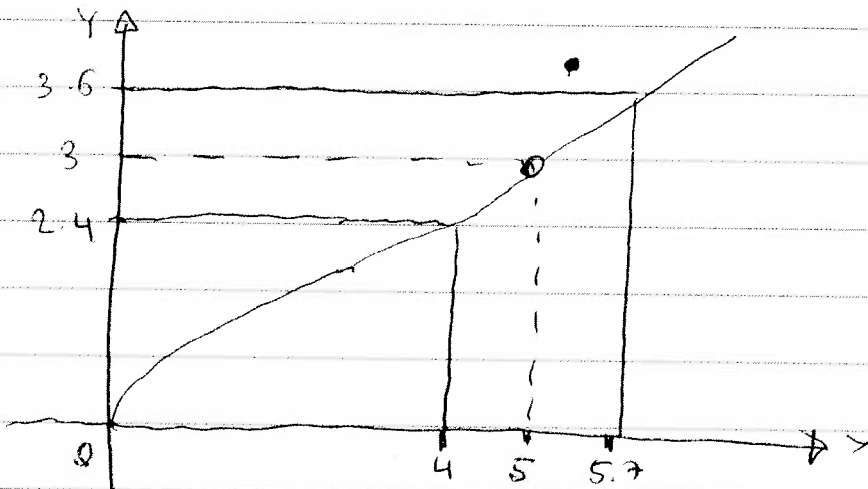
$x=4$ on the left

$$|x-5| < |4-5| = 1$$

$x=5.7$ on the right

$$|x-5| < |5.7-5| = .7$$

$\delta = 0.7$ or smaller



2.4
#15

We Love Math

Krystina
Jessica
Stephanie

Section 2.4

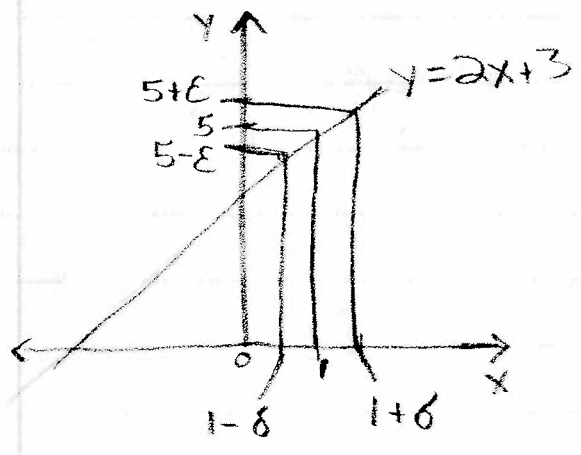
15. $\lim_{x \rightarrow 1} (2x+3) = 5$

If $0 < |x-1| < \delta$, then

$|2x+3-5| < \epsilon \rightarrow |2x-2| < \epsilon \rightarrow 2|x-1| < \epsilon \rightarrow |x-1| < \frac{\epsilon}{2}$

so if we choose $\delta = \frac{\epsilon}{2}$, then $0 < |x-1| < \delta \rightarrow |2x+3-5| < \epsilon$.

By definition of a limit $\lim_{x \rightarrow 1} (2x+3) = 5$



24
#15a

ϵ

$$\lim_{x \rightarrow 2} (4 + 2x) = 6$$

$$|4 + 2x| < 6$$

$$= |2x + 4 - 6| < \epsilon$$

$$|2x - 2| < \epsilon$$

$$2|x - 1| < \epsilon$$

$$|x - 1| < \frac{\epsilon}{2} \quad \delta < \epsilon/2$$

Sal J.
Fabian Best

2.4
#18

Team Kickass

2.4 #18

$$\lim_{x \rightarrow 4} (7 - 3x) = -5$$

$$|-3x + 7 - (-5)| < \epsilon$$

$$|-3x + 12| < \epsilon$$

$$\frac{|-3||x-4|}{3} < \frac{\epsilon}{3}$$

$$\delta < \frac{\epsilon}{3}$$

(2.4)
#20

Science Buddies

#20

$$\lim_{x \rightarrow 6} \left(\frac{x}{4} + 3 \right) = \frac{9}{2}$$

$$\left| \frac{x}{4} + 3 - \frac{9}{2} \right| < \epsilon$$

$$\left| \frac{x}{4} + \frac{(6-9)}{2} \right| < \epsilon$$

$$\left| \frac{x}{4} - \frac{3}{2} \right| < \epsilon$$

$$\frac{1}{4} |x - 6| < \epsilon$$

$$|x - 6| < 4\epsilon$$

$$\delta = 4\epsilon$$

$$= \frac{1}{4} |x - 6| < \delta$$

$$\frac{1}{4} \cdot \delta$$

$$\frac{1}{4} \cdot 4\epsilon$$

(2.4 #20) Letrice
Wilgens
Viviene

L. W. V.

02/8/10

2.4

20.

$$\lim_{x \rightarrow 6} \left(\frac{x}{4} + 3 \right) = \frac{9}{2}$$

$$0 < |x - 6| < \delta \quad \text{then} \quad \left| \left(\frac{x}{4} + 3 \right) - \frac{9}{2} \right| < \varepsilon$$

$$\text{but } \left| \left(\frac{x}{4} + 3 \right) - \frac{9}{2} \right| \Rightarrow \frac{x}{4} + \left(\frac{3-9}{2} \right) = \left| \frac{x-3}{4} \right| = \left| \frac{1}{4}(x-6) \right| = \frac{1}{4}|x-6|$$

$$\text{if } 0 < |x-6| < \delta \quad \text{then} \quad \frac{1}{4}|x-6| < \varepsilon \times 4$$

$$\text{that is if } 0 < |x-6| < \delta \quad \text{then} \quad |x-6| < 4\varepsilon$$

$$\delta = 4\varepsilon$$

Given $\varepsilon > 0$; $\delta = 4\varepsilon$. If $0 < |x-6| < \delta$ then

$$\left| \left(\frac{x}{4} + 3 \right) - \frac{9}{2} \right| = \left| \frac{x-3}{4} \right| = \frac{1}{4}|x-6| < \frac{\delta}{4} = \frac{1}{4}(4\varepsilon) = \varepsilon$$

Thus $0 < |x-6| < \delta$ then $\left| \left(\frac{x}{4} + 3 \right) - \frac{9}{2} \right| < \varepsilon$

therefore,

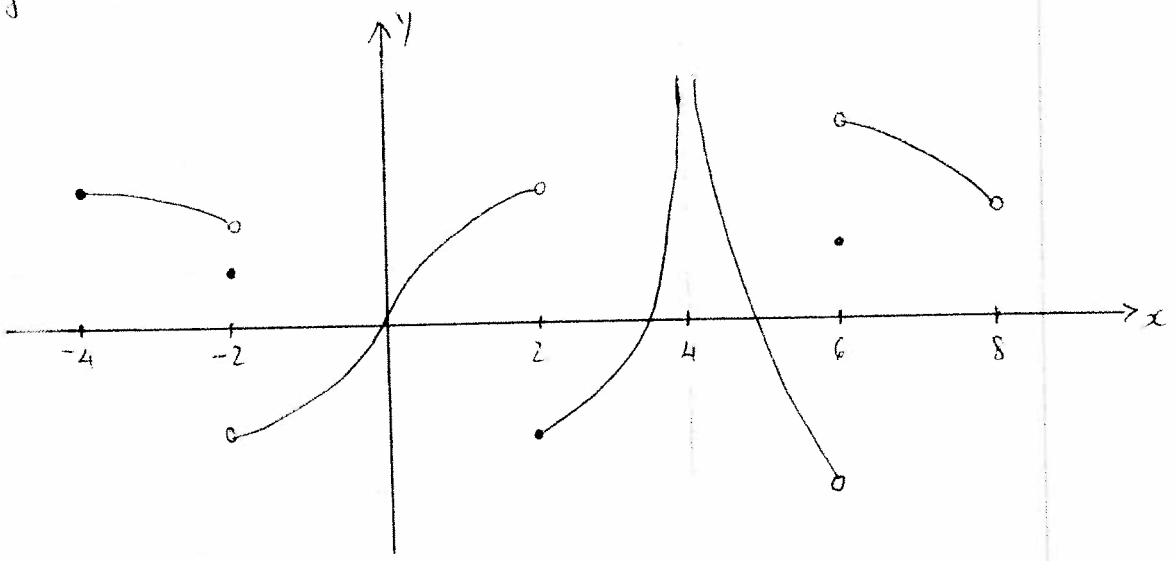
$$\lim_{x \rightarrow 6} \left(\frac{x}{4} + 3 \right) = \frac{9}{2}.$$

2.5-4/128

From the graph of g , state the intervals on which g is continuous.

Vinh Le
Ioan
Mike

25
HW4



g is continuous on $[-4, -2)$
 $(-2, 2)$
 $(2, 4)$
 $(4, 6)$
 $(6, 8)$

FR3CH

2.5
#12

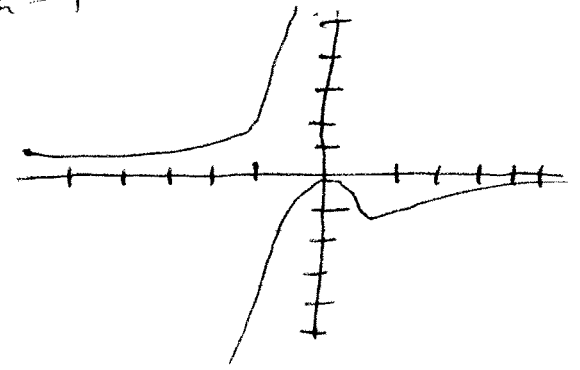
Abc Eger
YES MOSCOW

THE GROUP - Section 2.5 #12

Feb. 8, 2010

#12 $h(t) = (2t - 3t^2) \div (1 + t^3), a = 1$

- 1. $f(a)$ is define ✓
- 2. $\lim_{x \rightarrow a} f(x)$ exist ✓
- 3. $\lim_{x \rightarrow a} f(x) = f(a)$ ✓

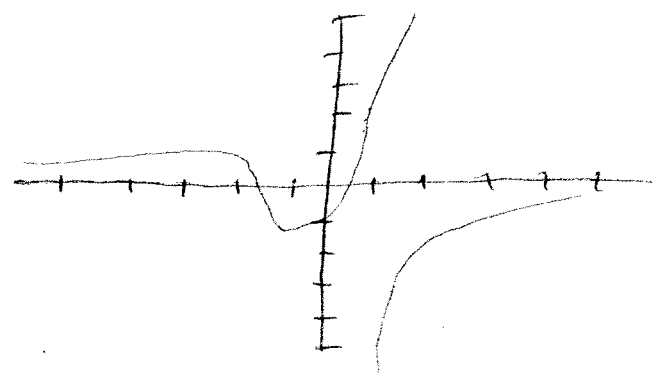


* polynomials is continuous everywhere except where $1 + t^3 = 0$

↳ continuous @ $c = 1$

#12a $h(t) = (8t + 5t^2) \div (3 - t^3), a = 1$

- 1. $f(a)$ is define ✗
- 2. $\lim_{x \rightarrow a} f(x)$ exist ✗
- 3. $\lim_{x \rightarrow a} f(x) = f(a)$ ✗



* polynomial is continuous everywhere except where $3 - t^3 = 0$

Not continuous @ $a = 1$

2.5
#13
2.5

$$13. f(x) = \frac{2x+3}{x-2}, \quad (2, \infty)$$

1. $f(a)$ is defined if $x \neq 2$

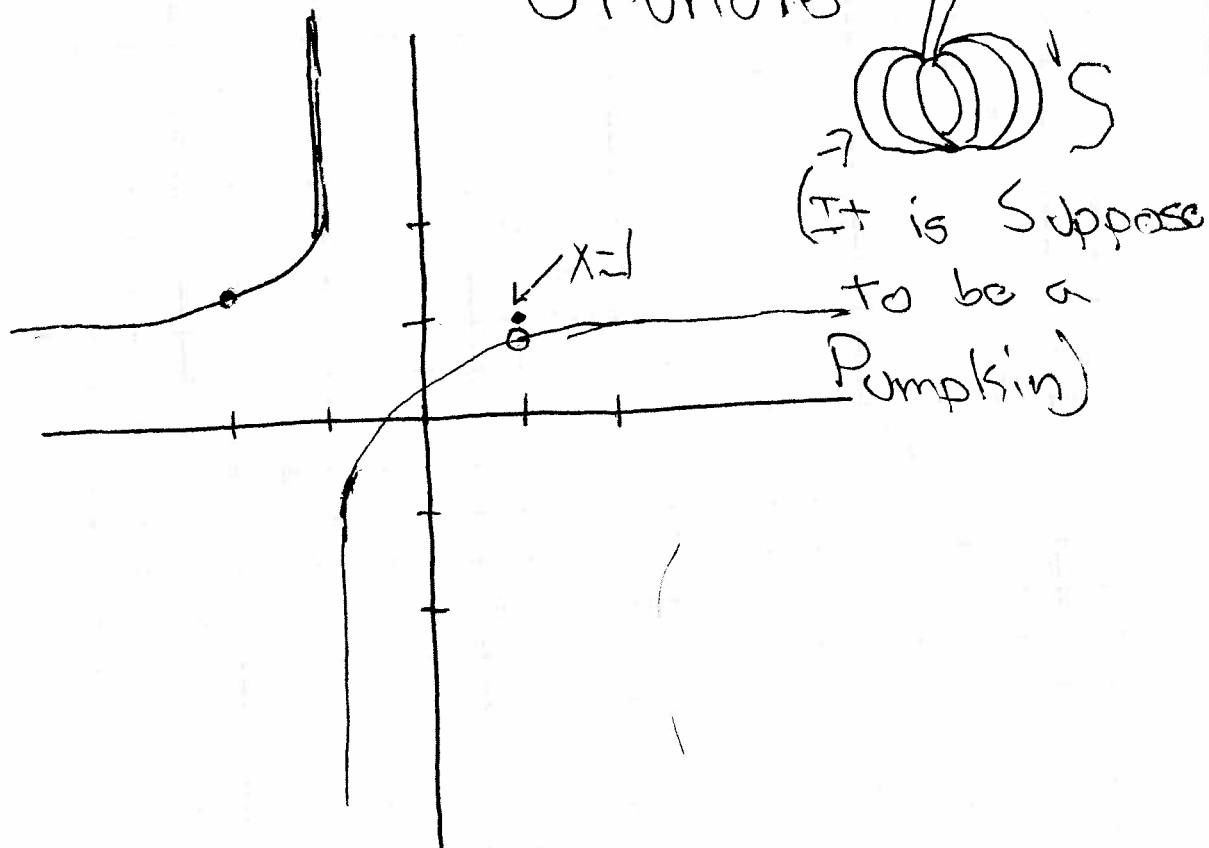
2. $\lim_{x \rightarrow a} f(x)$ exists if $x \neq 2$

3. $\lim_{x \rightarrow a} f(x) = f(a)$

2.5
#18

$$f(x) = \begin{cases} \frac{x^2-x}{x^2-1} & \text{if } x \neq 1 \\ 1 & \text{if } x = 1 \end{cases}$$

Grundle



With $(1 \text{ if } x=1)$ acting as a "plug", inputting 1 within

$$\frac{x^2-x}{x^2-1} = \frac{x(x-1)}{(x-1)(x+1)} = \frac{1}{x+1} = \frac{1}{2} \text{ and}$$

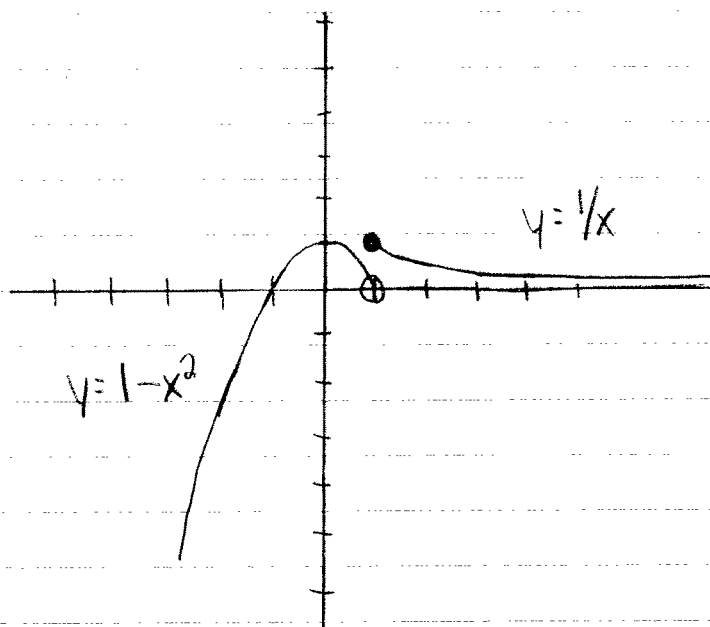
It would not "insert" into the missing plot due to the fact that $\frac{1}{2} \neq 1$ so it is

Discontinuous.

2.5
#17

Kristian Fehrer, Mehra Avila, Jalisha Crews Save the Polar Bears
Mat: 151
HW: 2.4-2.5

$$2.5 \text{ #17. } f(x) = \begin{cases} 1-x^2 & \text{if } x < 1 \\ 1/x & \text{if } x \geq 1 \end{cases} \quad a=1 \quad \text{as } x \rightarrow a \dots$$

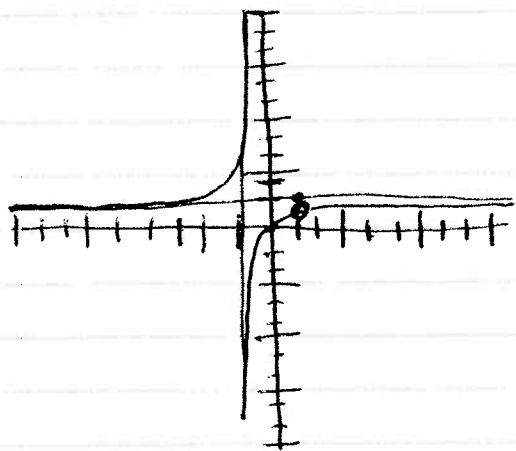


At $a=1$, $f(x)$ is discontinuous because the limit of $f(x)$ as x approaches a does not exist; this is due to differences in the left and right limits.

2.5
#18

Diesel

Connor Payne Tyler Ferst Stanley Tucher



$$f(x) = \begin{cases} \frac{x^2 - x}{x^2 - 1} & \text{if } x \neq 1 \\ 1 & \text{if } x = 1 \end{cases} \quad a = 1$$

It is discontinuous at $x = -1$ because there is an asymptote error.

It is discontinuous at $x = 1$ because $x \neq 1$ in $y = 1$.

$$\frac{x^2 - x}{x^2 - 1} = \frac{x(x-1)}{(x-1)(x+1)} = \frac{x}{x+1}$$

The function is discontinuous because there is a hole at $x = 1$ in the first function and the second function does not plug in the hole left by the first function because it is placed above it at the horizontal asymptote $y = 1$.

2.5
#35

Ryan ZHAO

Will Arbeta

BA IS ~~AA~~ BS

$$f(x) = \begin{cases} x^2 & \text{if } x < 1 \\ \sqrt{x} & \text{if } x \geq 1 \end{cases}$$

$$\lim_{x \rightarrow 1^-} f(x) = 1$$

$$\lim_{x \rightarrow 1^+} f(x) = 1$$

$f(x)$ is continuous

Because the function meets
the definition of limit.

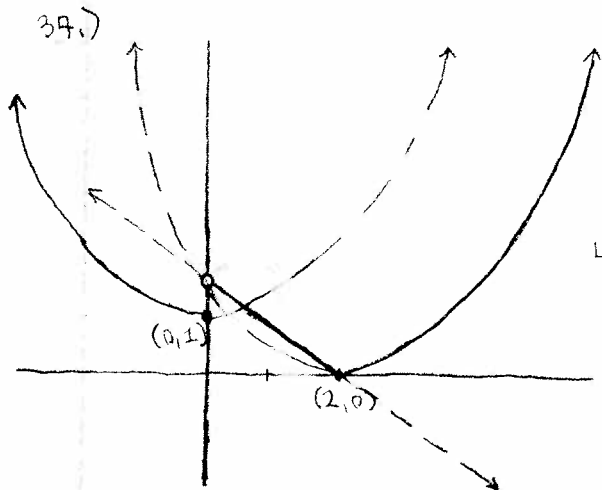
25
#37

MAT151...

2.5 #37

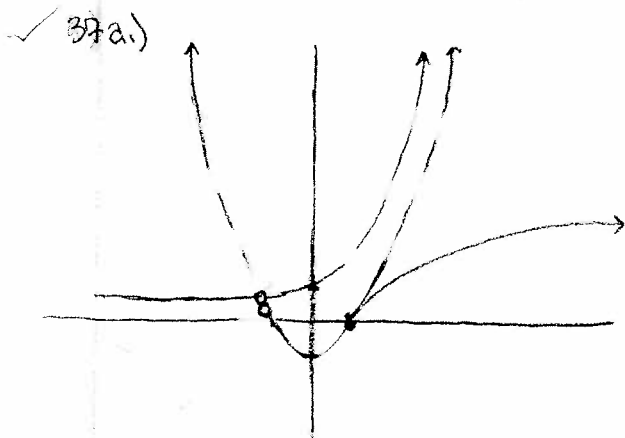
Team: G

Jonathan Chen
Guan Zheng
Mire Bank



$$f(x) = \begin{cases} 1+x^2 & \text{if } x \leq 0 \\ 2-x & \text{if } 0 < x \leq 2 \\ (x-2)^2 & \text{if } x > 2 \end{cases}$$

L $f(x)$ is discontinuous at (0) , ...
from the left.



$$f(x) = \begin{cases} x^2-1 & \text{if } -1.315 < x \leq 1 \\ \sqrt{x-1} & \text{if } x > 1 \\ e^{x+1} & \text{if } x < -1.315 \end{cases}$$

L $f(x)$ is discontinuous at
 -1.315 from the left
(removable discontinuity)

25
#45

SECTION 2.5
PROB #45

CIV. ARC
JASON KOHLHEP
RYAN DSOJKA
STEPHEN MANCE

45 IF $f(x) = x^2 + 10 \sin x$, SHOW THAT THERE IS A NUMBER 'c' SUCH THAT $f(c) = 1000$

$$f(x) = x^2 + 10 \sin x = 1000$$

$f(x)$ CONTINUOUS EVERYWHERE

$$f(31) = 956$$

$$f(32) = 1029$$

BY IVT, THERE IS A 'c'

$$f(c) = 1000 \text{ SO } c^2 + 10 \sin c = 1000$$

2.5
#47a

TEAM: C.A.M

47a.

$$x^4 + x - 3 = 0 \quad (1, 2)$$

$$f(1) = (1)^4 + 1 - 3 = 0$$

$$1 + 1 - 3 = -1 < 0$$

$$f(2) = (2)^4 + 2 - 3 = 0$$

$$16 + 2 - 3 = 0$$

$$16 - 3 = 13 > 0$$

polynomial or f

is continuous

everywhere