

2.10.2



Use the mean value theorem:

$$f(x) = x^2 + 1, \quad [0, 2] \quad \text{Find Number } 'c'$$

$$f'(x) = 2x \quad \therefore \text{there is a number } 'c' \text{ in } [0, 2]$$

$$f'(c) = \frac{f(2) - f(0)}{2 - 0} = \frac{4}{2} = 2$$

TO Find 'c' - We set:

$$f'(c) = 2c = 2$$

so $c = \frac{2}{2} = 1$

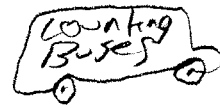
2, 10 - 2

$$2. f(x) = x^2 + 1, [0, 2]$$

$$f'(c) = \frac{f(2) - f(0)}{2 - 0} =$$

$$2c = \frac{5 - 1}{2 - 0} = 2$$

$$c = 1$$



HW
#9

D G K

$$4) f(x) = x^3 + x^2 \quad [-1, 1]$$

$$f'(c) = \frac{f(1) + f(-1)}{1+1} = \frac{2+0}{2} = 1$$

$$f'(1) = 3x^2 + 2x = 1$$

$$3(-1)^2 + 2(-1) =$$

$$3 - 2 = 1$$

$$3x^3 + 2x^2 - 1 = 0$$

$$= \frac{-2 \pm \sqrt{2^2 - 4(3)(-1)}}{2(1)} =$$

$$= \frac{-2 \pm \sqrt{4 - 12}}{2}$$

$$= \frac{-2 \pm \sqrt{-8}}{2}$$

Doubts Helix

HW#10

p. 208 # 84

Find a value of c as guaranteed by the Mean Value Theorem.

$$f(x) = x^3 - x \text{ on interval } [0, 2]$$

$$f'(c) = \frac{f(2) - f(0)}{2 - 0} = \frac{(2^3 - 2) - (0^3 - 0)}{2} = \frac{6}{2} = 3$$

$$f'(c) = \frac{d}{dx}(c^3 - c)$$

$$f'(c) = 3c^2 = 3$$

$$c = 1$$

$$c = \sqrt{1}$$

$c = 1$ b/c it's between $[0, 2]$

$$\#2) f(x) = (x+1)^{\frac{1}{3}} \quad x_0 = 0; \overline{0.2}$$

$$f(0) = (0+1)^{\frac{1}{3}}$$

$$\underline{f(0) = 1} \quad (0; 1)$$

$$f'(x) = \frac{1}{3} (x+1)^{-\frac{2}{3}}$$

$$f'(0) = \frac{1}{3} = "$$

$$y - 1 = \frac{1}{3} (x - 0)$$

$$y = \frac{1}{3}x + 1$$

$$y(0.2) = \frac{1}{3} \cdot (0.2) + 1$$

$$= 1.0666$$

from calc 1.062

INVESTMENT BANKERS

3.1 Use linear approximation to estimate the quantity.

8. (a) $\sin(0.1)$ (b) $\sin(1.0)$ (c) $\sin\left(\frac{9}{4}\right)$

a. Find the linear approximation of $f(x) = \sin x$, at $x_0 = 0$.

$$f(x) = f(x_0) + f'(x_0)(x - x_0)$$

$$f(0.1) = \sin(0) + \cos(0)(0.1 - 0)$$

$$f(0.1) = 0 + 1(0.1)$$

$$f(0.1) = 0.1$$

b. Find the linear approximation of $f(x) = \sin x$, at $x_0 = \frac{\pi}{3}$.

$$f(x) = f(x_0) + f'(x_0)(x - x_0)$$

$$f(1.0) = \sin\left(\frac{\pi}{3}\right) + \cos\left(\frac{\pi}{3}\right)\left(1.0 - \frac{\pi}{3}\right)$$

$$f(1.0) = \frac{\sqrt{3}}{2} + \frac{1}{2}(-0.04719 \dots)$$

$$f(1.0) \approx 0.84242 \dots$$

c. Find the linear approximation of $f(x) = \sin x$, at $x_0 = \frac{3\pi}{4}$.

$$f(x) = f(x_0) + f'(x_0)(x - x_0)$$

$$f\left(\frac{9}{4}\right) = \sin\left(\frac{3\pi}{4}\right) + \cos\left(\frac{3\pi}{4}\right)\left(\frac{9}{4} - \frac{3\pi}{4}\right)$$

$$f\left(\frac{9}{4}\right) = \frac{\sqrt{2}}{2} + \left(-\frac{\sqrt{2}}{2}\right)(-0.10619 \dots)$$

$$f\left(\frac{9}{4}\right) \approx 0.78219 \dots$$

Section 3.1

i.t.

14

Use Newton's method with the given X_0 to(a) compute X_1 and X_2 by hand and (b)

Use a calculator to find the root to

At least five decimal places of accuracy

$$X^3 + 4x^2 - x - 1 = 0 \quad X_0 = -1$$

$$= X_n - \frac{X_n^3 + 4X_n^2 - X_n - 1}{3X_n^2 + 8X_n - 1}$$

$$X_1 = -5 \quad X_1 = -5 - \frac{(-5)^3 + 4(-5)^2 - (-5) - 1}{3(-5)^2 + 8(-5) - 1} = -4.36235\dots$$

$$X_2 = -7.4 \quad X_2 = -7.4 - \frac{(-7.4)^3 + 4(-7.4)^2 - (-7.4) - 1}{3(-7.4)^2 + 8(-7.4) - 1} = -4.18207\dots$$

$$X_3 = -4.1$$

trunc
calc

$$\text{Root} = -4.18194\dots$$

16) MAT Finisher

~~$f(x) = \sin 3x, x_0 = 0, \sin(0, 3)$~~

Equation of line tangent to $y = x^2 - 9$

$L_1: y + 8 = 2(x - 1) \quad y' = 2x$

$y = 2(x - 1) - 8 \quad m = y'(1) = 2$

point $(1, -8)$

Zero for L_1

$0 = 2(x - 1) - 8$

$8 = 2(x + 1)$

$4 = x + 1$

$5 = x$

M. ~~Shi~~

Hiroaki Tomioka

PURPLE PARROTS

3.1

$$32. 4x^3 - 7x^2 + 1 = 0 \quad x_0 = 1$$

Newton's Method

$$x_0 - \frac{f(x_0)}{f'(x_0)}$$

H.W

X - July

$$3.2 = \boxed{6}.$$

$$\boxed{6} \lim_{t \rightarrow 0} \frac{\sin t}{e^{3t} - 1}$$

$$\lim_{t \rightarrow 0} \frac{\frac{d}{dx} \sin t}{\frac{d}{dx} e^{3t} - 1}$$

$$= \lim_{t \rightarrow 0} \frac{\cos t}{e^{3t}}$$

$$= \frac{\cos(0)}{e^{3(0)}}$$

$$= \frac{1}{1}$$

$$= \boxed{1}.$$

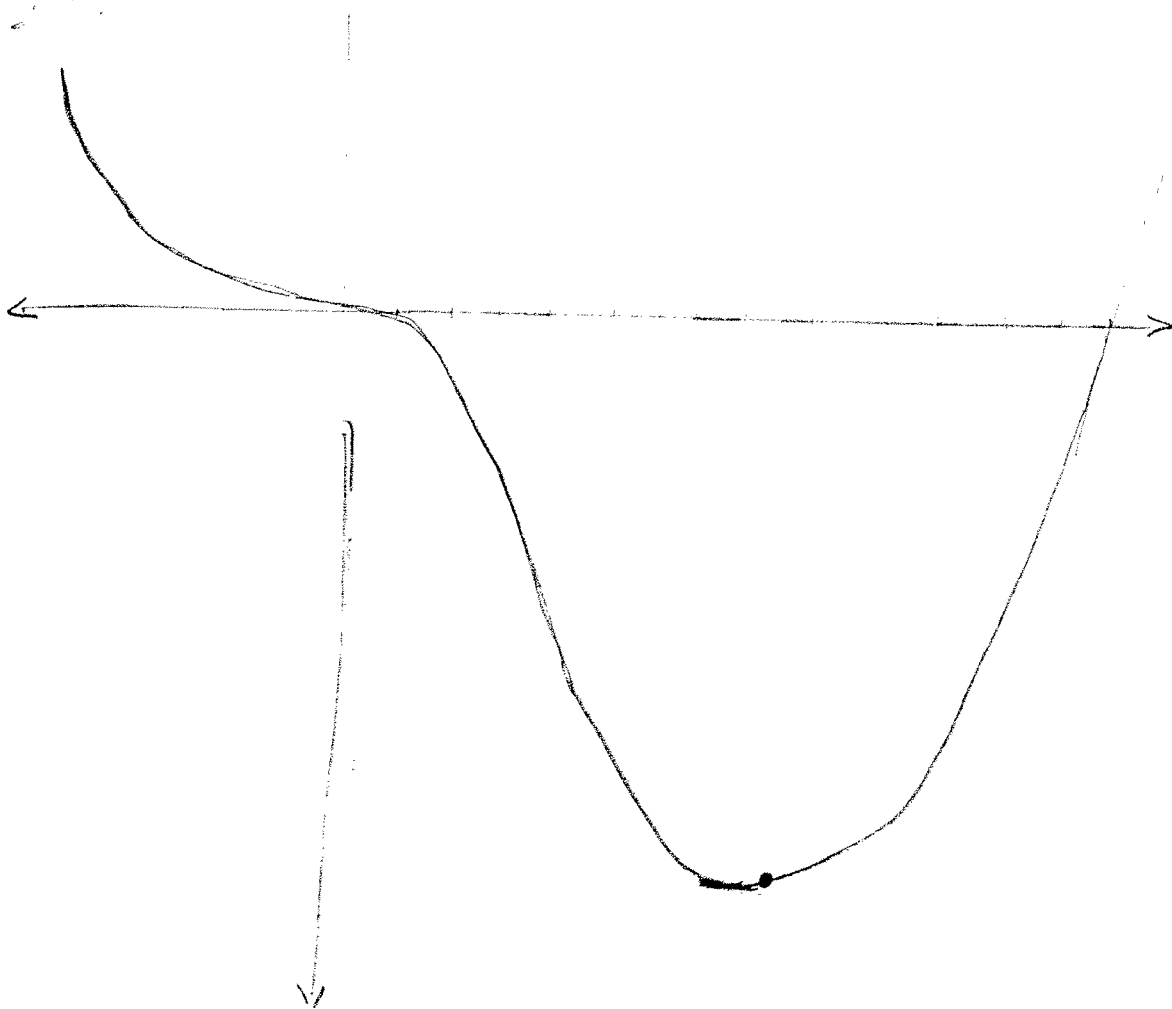
Abraham Sherman

Biologists

Timothy Lukowicz

Approximate the x-coordinates and sketch

21. $y_1 = x^4 - 16x^3 - 0.1x^2 + 0.5x - 1$



2ND CALC MINIMUM

$x_{max} = 12.003299$