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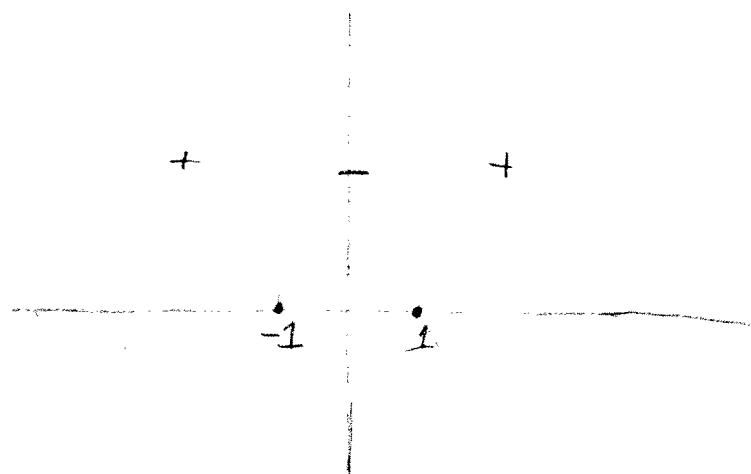
(Homework #11)

2)  $f(x) = x^4 - 6x^2 + 2x + 3$  find inflection points and when the graph is concave up and down

$$f'(x) = 4x^3 - 12x + 2$$

$$f''(x) = 12x^2 - 12$$

$$f''(x) = 0 \quad 12x^2 - 12 = 0 \\ x^2 = 1 \\ x = \pm 1$$



$$f''(2) = 12(2)^2 - 12 = 36 \quad (\text{positive})$$

$$f''(0) = 12(0)^2 - 12 = -12 \quad (\text{negative})$$

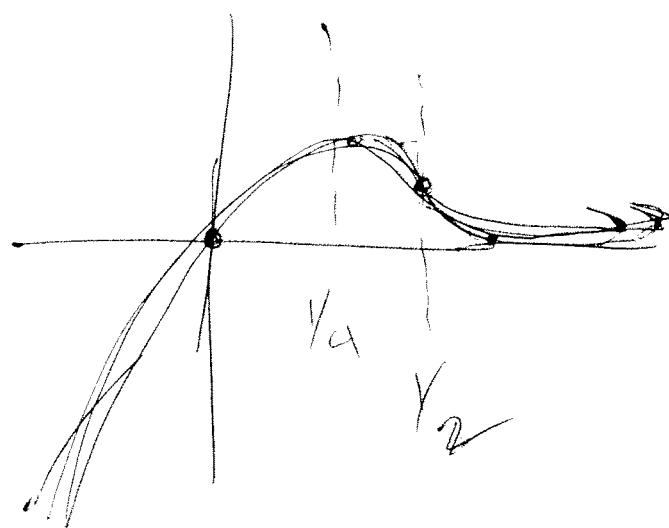
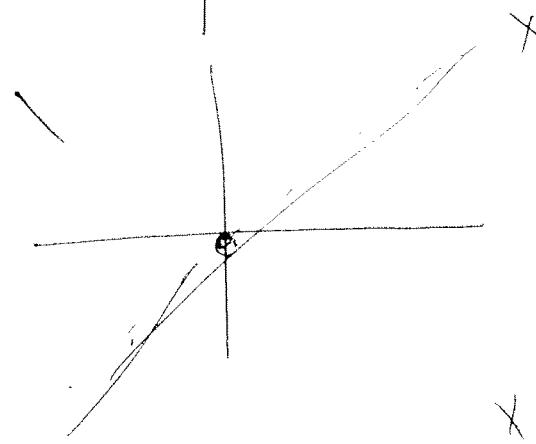
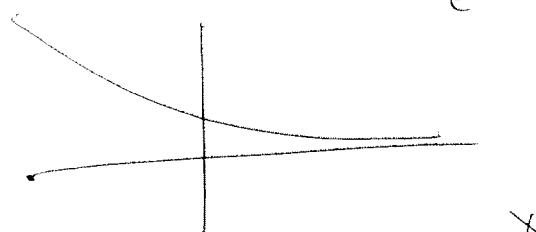
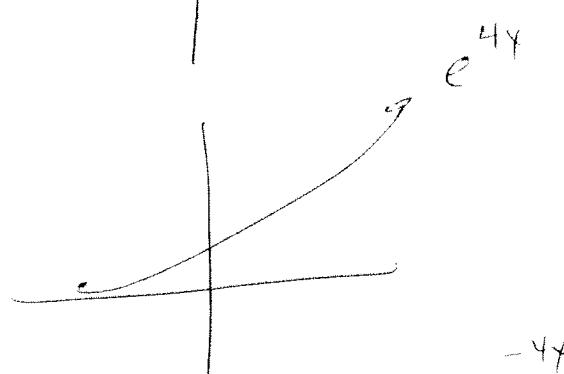
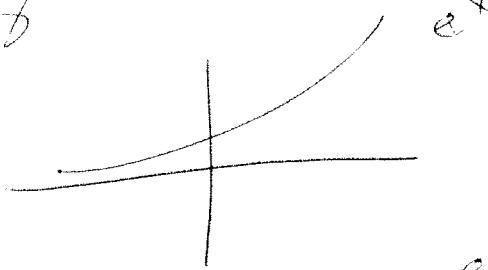
$$f''(-2) = 12(-2)^2 - 12 = 36 \quad (\text{positive})$$

inflection points:  $x = 1, -1$

concave up:  $(-\infty, -1) \cup (1, \infty)$

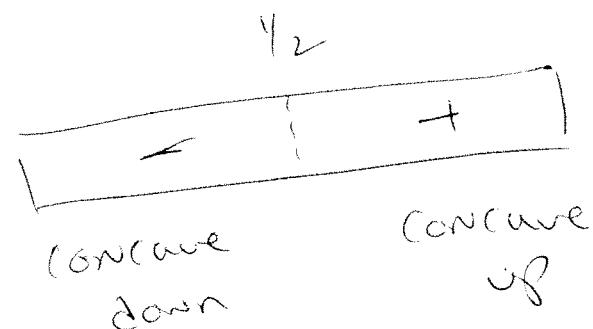
concave down:  $(-1, 1)$

# 8



$$\begin{aligned}
 y &= xe^{-4x} \\
 y' &= x(-4)e^{-4x} + e^{-4x} \\
 &= e^{-4x}(1-4x) \underset{x=1/4}{=} 0 \text{ MAX} \\
 y'' &= e^{-4x}(-4) + (1-4x)(-4)e^{-4x} \\
 &= e^{-4x}(-4 + 16x) \\
 &= 0 \quad \Rightarrow \quad -4 + 16x = 0 \\
 &\Rightarrow x = \frac{1}{4}
 \end{aligned}$$

$$\begin{aligned}
 y &= 16x \\
 x &= \frac{1}{2} \quad \text{INFLECTION POINT}
 \end{aligned}$$



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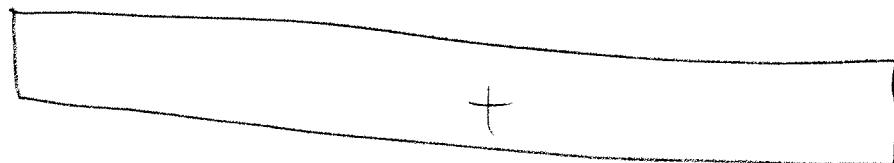
Ma.T - Finishers

Sketch a graph with the given properties

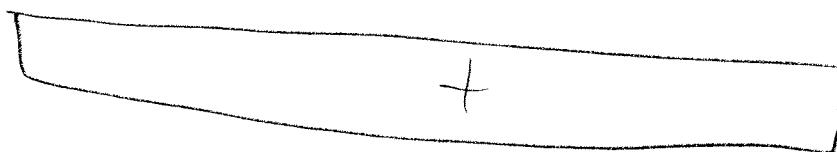
$f(0) = 2$ ,  $f'(x) > 0$  for all  $x$ ,  $f'(0) = 1$ ,  $f''(x) > 0$  for  $x < 0$ ,

$f''(x) \leq 0$  for  $x > 0$

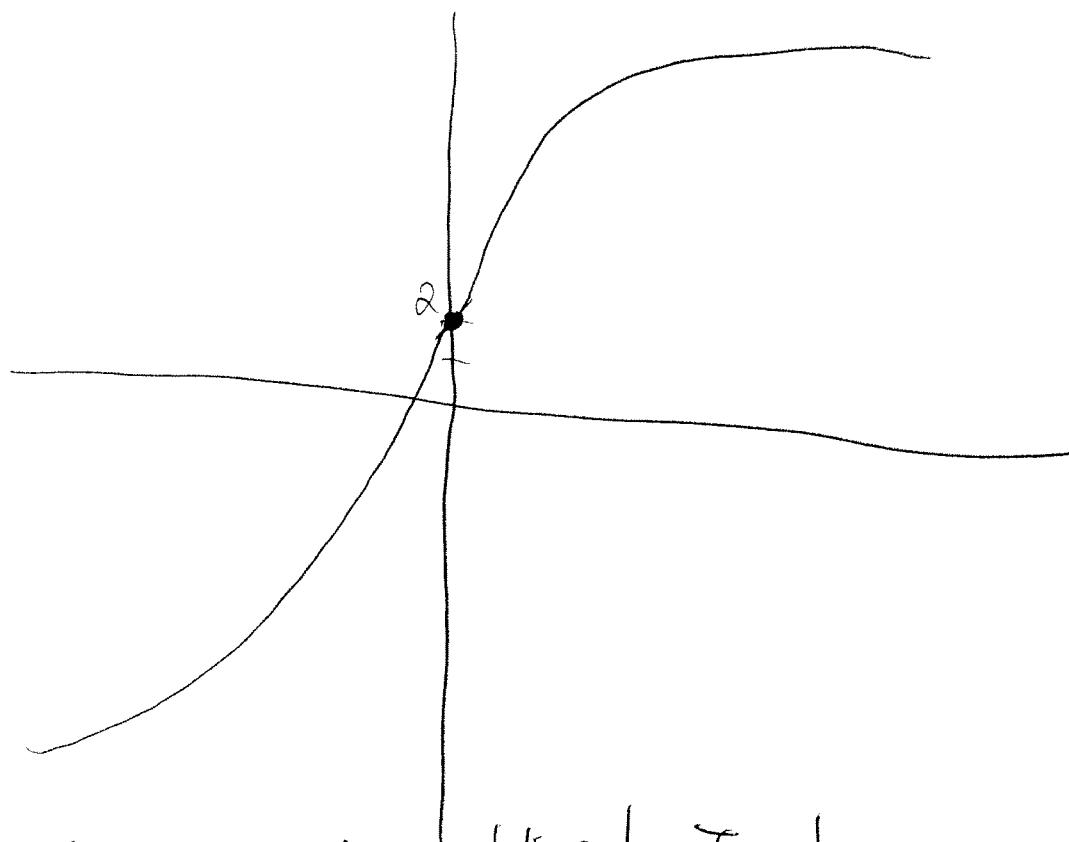
$f(0)$



$f'(0)$



$f''(0)$



M.  
Shy

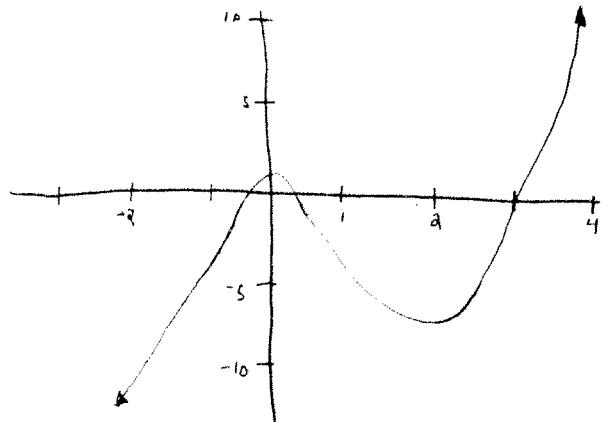
Julian Ward

Hiroaki Tomonaga

## Section 3.5

#46

it

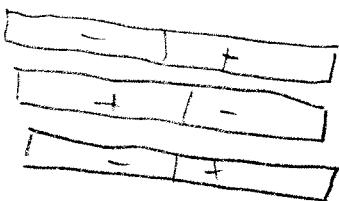
 Gradyan Rogay  
 Part Vell  
 Mo Sly


estimate the intervals of increase and decrease, the location of local extrema, intervals of concavity and locations of inflection points

Local MAX At  $x=0$

Local Min At  $x=a$

inflection point At  $x=1$



## INVESTMENT BANKERS

3.6

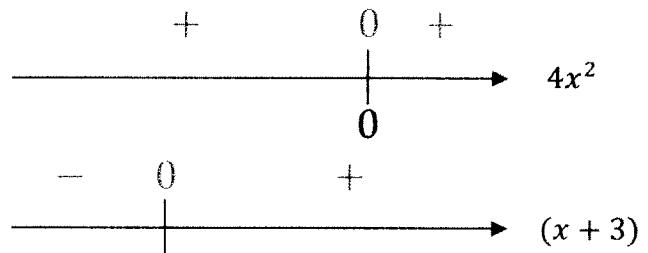
$$4. \quad f(x) = x^4 + 4x^3 - 1$$

$$\begin{aligned} f'(x) &= 4x^3 + 12x^2 \\ &= 4x^2(x + 3) \end{aligned}$$

$$\begin{aligned} 4x^2 &= 0 & x + 3 &= 0 \\ x &= 0 & x &= -3 \end{aligned}$$

$$f'(x) \begin{cases} > 0, \text{on } (0, \infty) \\ < 0, \text{on } (-\infty, -3) \text{ and } (-3, 0) \end{cases}$$

LOCAL MIN :  $x = -3$

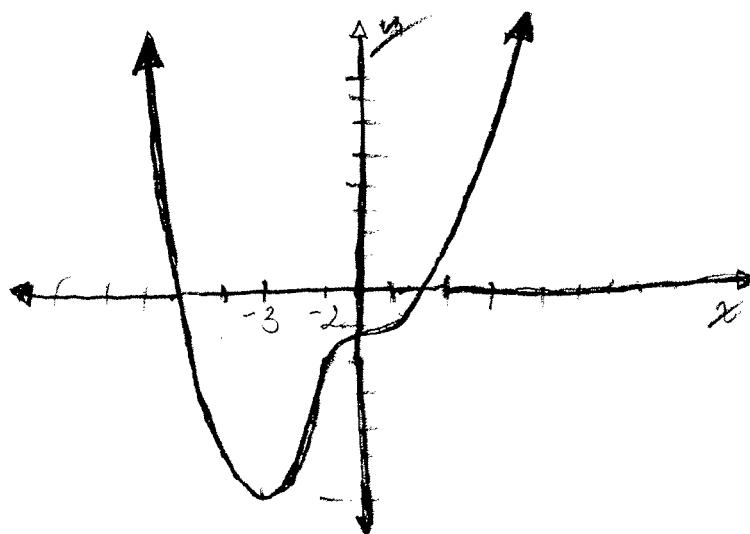
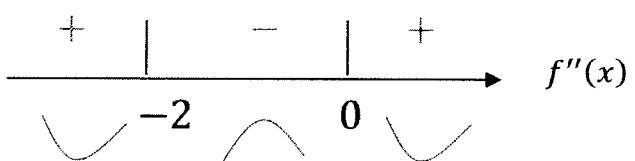
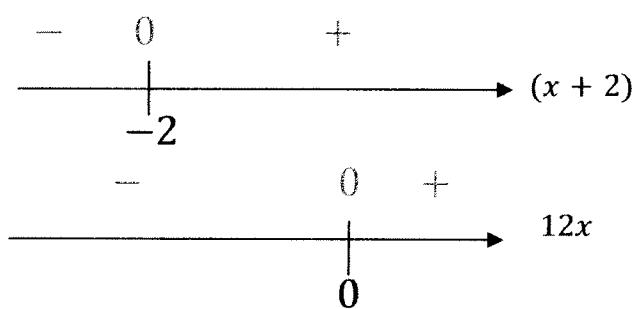


$$\begin{aligned} f''(x) &= 12x^2 + 24x \\ &= 12x(x + 2) \end{aligned}$$

$$\begin{aligned} 12x &= 0 & x + 2 &= 0 \\ x &= 0 & x &= -2 \end{aligned}$$

$$f''(x) \begin{cases} > 0, \text{on } (-\infty, -2) \text{ and } (0, \infty) \\ < 0, \text{on } (-2, 0) \end{cases}$$

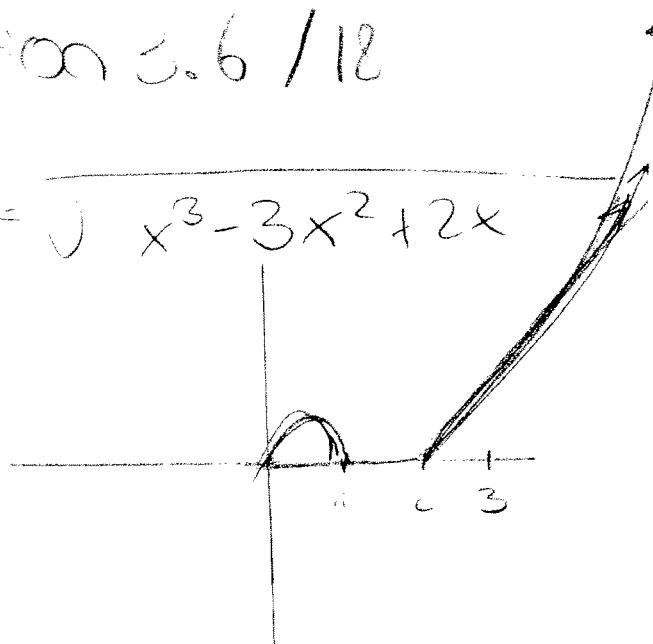
INFLECTION POINTS =  $x = -2, x = 0$



# Deutsche Produktion

Section 3.6 / 18

$$f(x) = \sqrt{x^3 - 3x^2 + 2x}$$



$$y = (\quad)^{\frac{1}{2}}$$

$$y' = \frac{1}{2}($$

$$\cdot (3x^2 - 6x + 2)$$

$$y'' = -\frac{1}{4}(\quad + \quad)$$

$$f(x)$$

0	1	2
0+	0+	pos
pos	pos	

zeros

$$y = x^{\frac{3}{2}}$$

$$y' = \frac{3}{2}x^{\frac{1}{2}}$$

$$y'' = \frac{3}{4}x^{-\frac{1}{2}} > 0$$

$$f'(x)$$

0	0.5	1	2	$\infty$
+	-		+	
inc	dec		inc	

Turning point

$$f''(x)$$

0	1	2	$\infty$
-		+	

Inflection Point

concave

down up

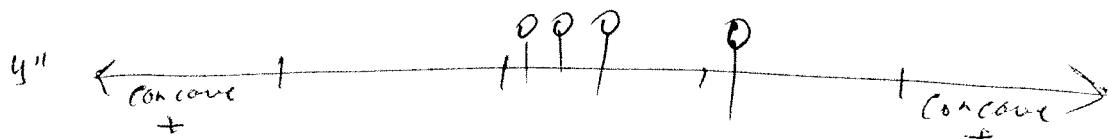
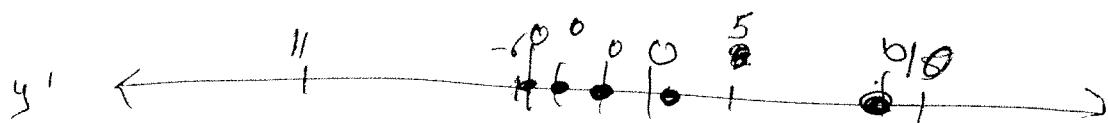
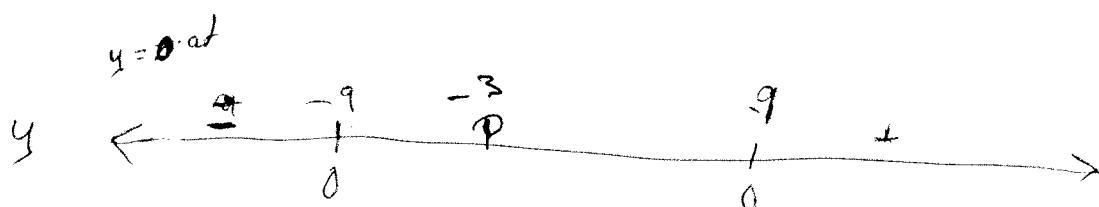
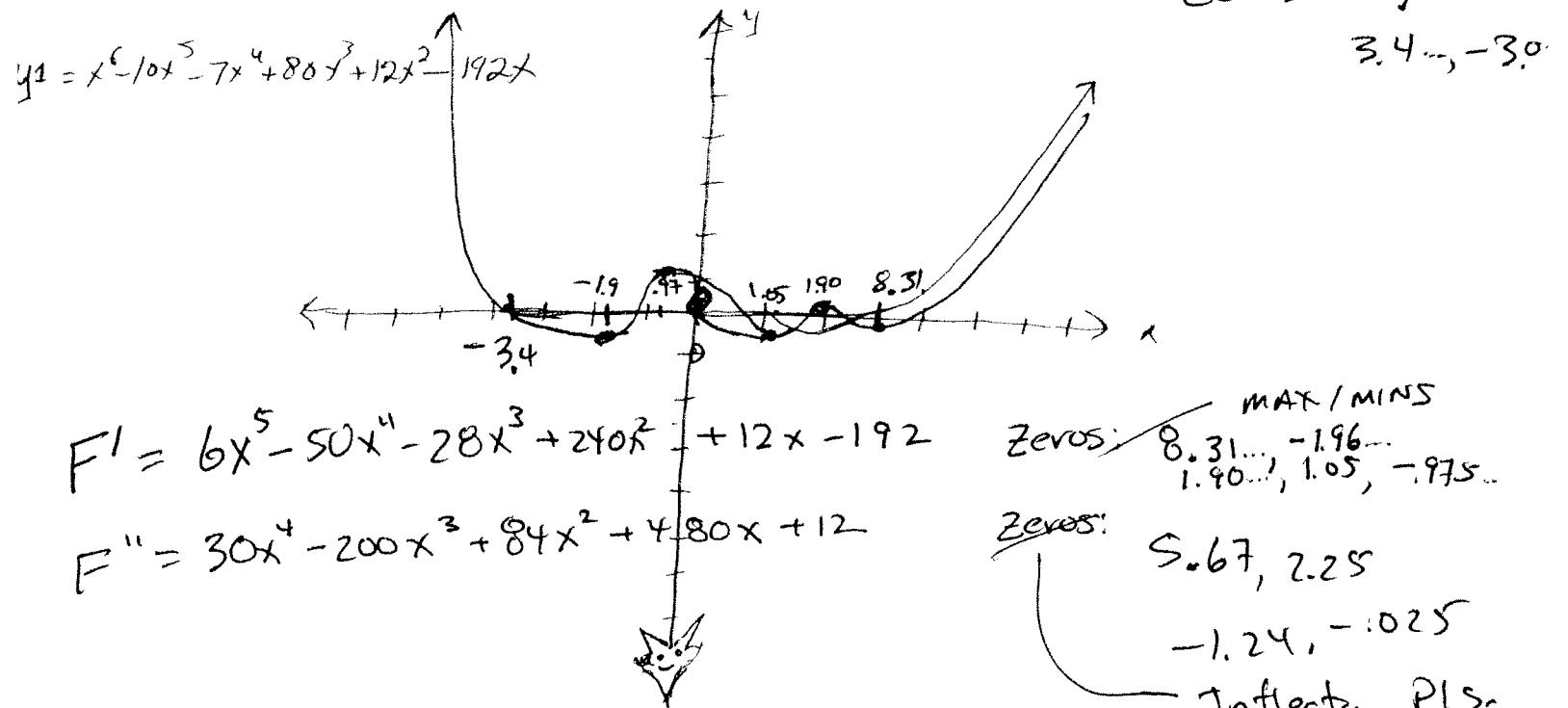
Determine All significant Features (approximately if necessary) and sketch a graph.

HELIX

# 26.  $F(x) = x^6 - 10x^5 - 7x^4 + 80x^3 + 12x^2 - 192x$

Zeros: 0, 9.8...

3.4..., -3.0



Function  $f$  has a slant asym  $y = mx + b (m \neq 0)$

If  $\lim_{x \rightarrow \infty} [f(x) - mx - b] = 0$  /  $\lim_{x \rightarrow -\infty} [f(x) - mx - b] = 0$

find slant asym. (use division to write function)  
then graph the function and its asymptote on same axes

$$y = \frac{(x-1)(x^2+x+1)}{(x-1)(x+1)}$$

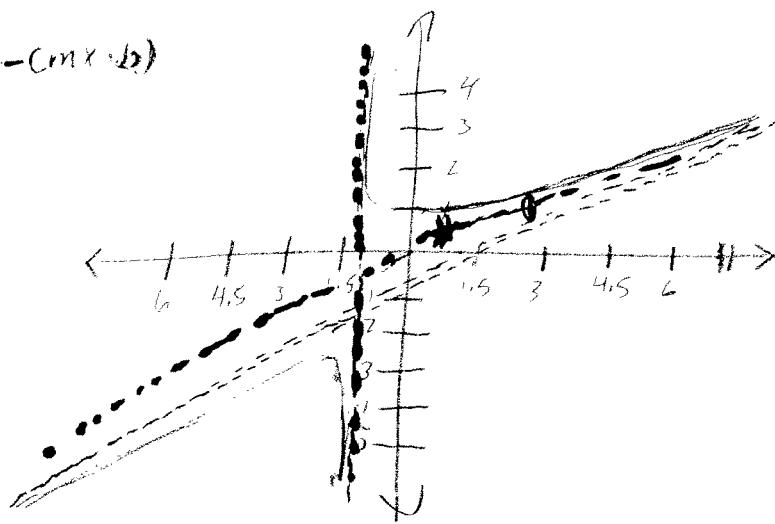


$$y = \frac{x^2+x+1}{x+1}$$

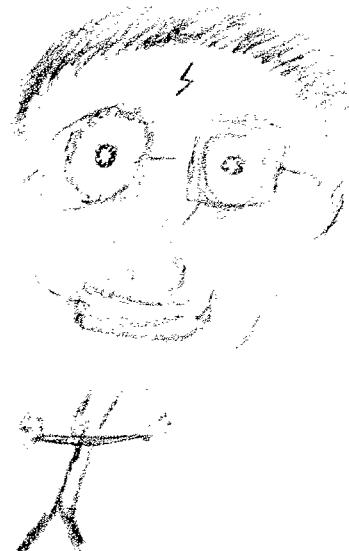
$$\frac{x^2+x+1}{x+1} = x + \frac{1}{x+1}$$

$$y = x \leftarrow \text{slant asymptote}$$

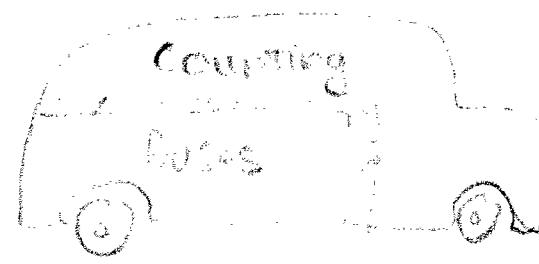
$$* = f(x) - (mx+b)$$



There is no  
 $\lim$   
to  $\infty$



Homework #1



3.6.50 find function whose graph has the given asymptotes.

$$x = 1, \underline{x = -1}, y = 0$$

We have: asymptotes:  $x = 1$ ,  $x = -1$  and  $y = 0$

$$\text{so: } f(x) = \frac{h(x)}{g(x)},$$

From:  $x = 1, x = -1$ : asymptotes:

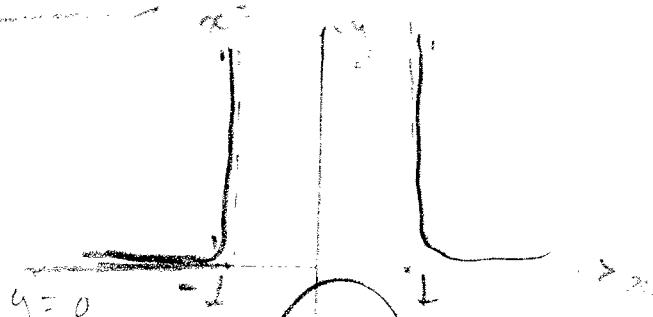
$$\Rightarrow g(x) = x + 1(x+1) = x^2 - 1$$

From:  $y = 0$  we know  $h(x) < g(x)$

$$\left\{ \begin{array}{l} \text{so } f(x) = \frac{ax+b}{x^2-1} \\ \quad x^2-1 \end{array} \right.$$

• guess  $a = 1, b = 2$ .

$$f(x) = \frac{x+2}{x^2-1}$$



• guess  $a = 0, b = 1$ .

$$f(x) = \frac{1}{x^2-1}$$