

3.2.16

$$\lim_{x \rightarrow \infty} \frac{e^x}{x^4}$$

$$= \lim_{x \rightarrow \infty} \frac{d}{dx} \frac{e^x}{x^4} = \lim_{x \rightarrow \infty} \frac{e^x}{4x^3} \quad \text{L'Hopital's Rule}$$

$$= \lim_{x \rightarrow \infty} \frac{d}{dx} \frac{e^x}{4x^3} = \lim_{x \rightarrow \infty} \frac{e^x}{12x^2} \quad \text{L'Hopital's Rule}$$

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$$= \frac{e^\infty}{24} = \frac{\infty}{24} = \infty$$

3.2-16

$$\lim_{x \rightarrow \infty} \frac{e^x}{x^4} \text{ use L'Hopital } \frac{\frac{d}{dx}(e^x)}{\frac{d}{dx}(x^4)} = \frac{\lim_{x \rightarrow \infty} e^x}{4x^3} \text{ use L'Hopital}$$

Counting Buses

$$\frac{\frac{d}{dx} e^x}{\frac{d}{dx} (4x^3)} = \frac{\lim_{x \rightarrow \infty} e^x}{12x^2} \text{ use L'Hopital } \frac{\frac{d}{dx}(e^x)}{\frac{d}{dx}(12x^2)} = \frac{\lim_{x \rightarrow \infty} e^x}{24x} \text{ use L'Hopital}$$

$$\frac{\frac{d}{dx}(e^x)}{\frac{d}{dx}(24x)} = \frac{\lim_{x \rightarrow \infty} e^x}{24} = \frac{\infty}{24} = \infty$$

# DGK

$$\#71 \quad \lim_{x \rightarrow \infty} \frac{(\sqrt{x^2+1} - x)}{1} \cdot \frac{\sqrt{x^2+1} + x}{\sqrt{x^2+1} + x}$$

$$\lim_{x \rightarrow \infty} \frac{x^2+1-x}{\sqrt{x^2+1}+x} = \frac{\infty}{\infty} \Rightarrow \cancel{0} \quad \text{use l'Hopital's rule}$$

$$\lim_{x \rightarrow \infty} \frac{2x-1}{\frac{1}{2}(x^2+1)^{-1/2}+1} = \frac{\infty}{1} = \infty$$

## Double Helix

3.2 # 38  $\Rightarrow$  Find the indicated limits.

$$\lim_{x \rightarrow 0^+} (\cos x)^{1/x}$$

$y = (\cos x)^{1/x}$  convert to logarithm.

$$e^{\ln y} = e^{1/x \ln(\cos x)}$$

$\hookrightarrow$  Hopital Rule

$$e^{\frac{-\frac{\sin(x)}{\cos(x)}}{1}} = e^{\frac{0}{1}} \rightarrow e^0$$

$$e^{\lim_{x \rightarrow 0^+} (\cos x)^{1/x}} = e^0 = 1$$

a)  $f(x) = x^3 - 3x + 1$

$f'(x) = 3x^2 - 3$

$0 = 3x^2 - 3$

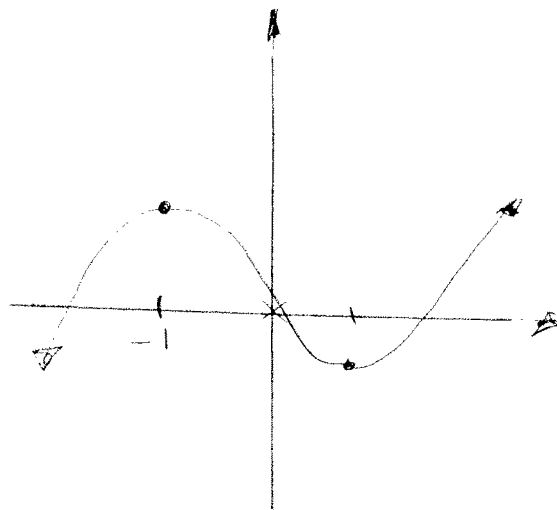
$0 = 3(x^2 - 1) \quad | :3$

$0 = (x^2 - 1) \quad | +1$

$1 = x^2 \quad | \sqrt{\quad}$

$x = \sqrt{1}$

$x_1 = 1$   
 $x_2 = -1$  Plug in  $f(x)$



max (-1; 3)

min (1; -1)

b)  $f(x) = -x^3 + 6x^2 + 2$

$f'(x) = -3x^2 + 12x$

$0 = -3x^2 + 12x$

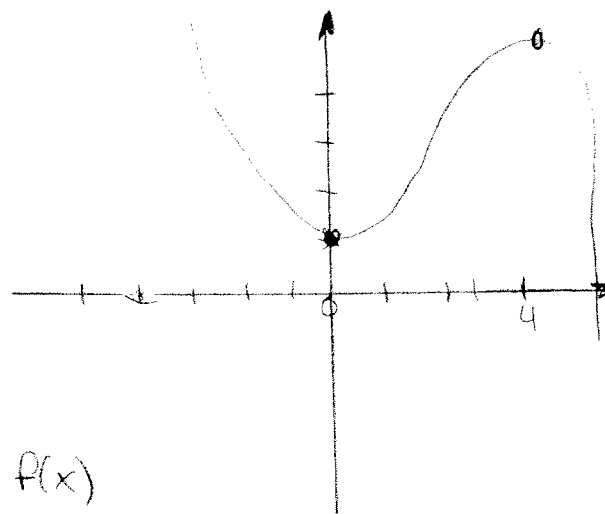
$0 = x(-3x + 12)$

↓

$x_0 = 0$   $0 = -3x + 12 \quad | -12$

$-12 = -3x \quad | (-3)$

$4 = x_0 \rightarrow$  plug in  $f(x)$



min (0; 2)

max (4; 34)

plug in  $f(x)$

# INVESTMENT BANKERS

3.3 Find all critical numbers by hand.

6. (a)  $f(x) = x^4 - 2x^2 + 1$       (b)  $f(x) = x^4 - 3x^2 + 2$

a.  $f(x) = x^4 - 2x^2 + 1$

$f'(x) = 4x^3 - 4x$

$f'(x) = 4x(x^2 - 1)$

~~$f'(x) = 4x(x+1)(x-1) = 0$~~

$4x = 0$

$x+1 = 0$

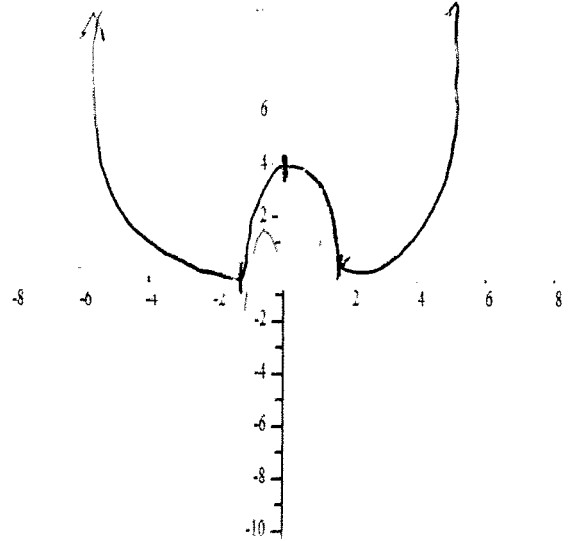
$x = -1$

$x-1 = 0$

$x = 1$

Critical Numbers:  $-1, 0, 1$        $-1, 1$  LOCAL MIN

$-1$  corresponds to a local Maximum       $0$  LOCAL MAX  
and  $1$  to a local Minimum.



b.  $f(x) = x^4 - 3x^3 + 2$

$f'(x) = 4x^3 - 9x^2$

~~$f'(x) = x^2(4x - 9) = 0$~~

$x^2 = 0$

$4x - 9 = 0$

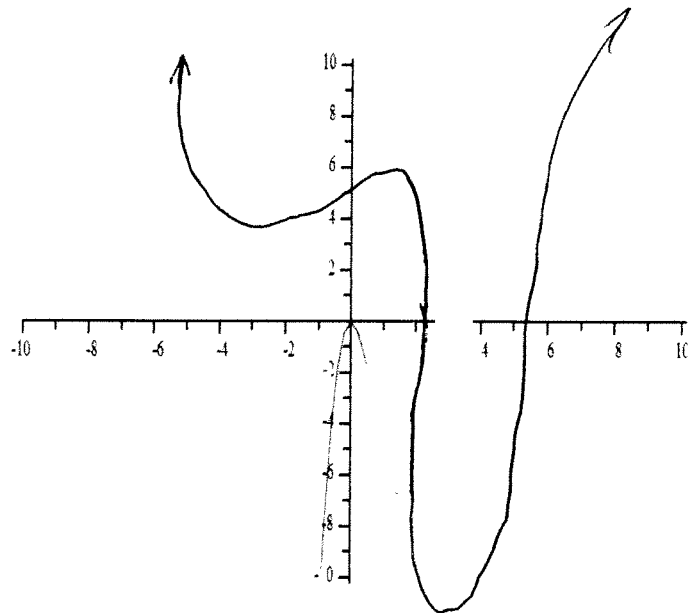
$x = 0$

$4x = 9$

$x = 2.25$

Critical Numbers:  $0, 2.25$

$0$  corresponds to a local Maximum and  $2.25$  corresponds to a local Minimum.



Section 3.3

.l.t.

find all critical #'s by hand  
use graph calc to see if they are  
either local min, max or neither

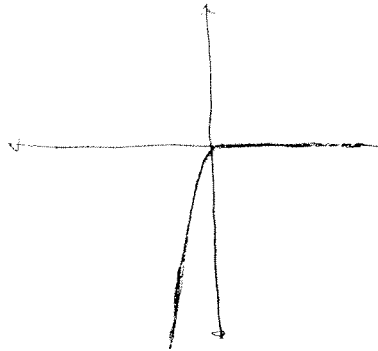
#16

$$f(x) = xe^{-ax}$$

$$f'(x) = \frac{dy}{dx} xe^{-ax}$$

$$= e^{-ax} \frac{d}{dx} - ax$$

$$f' = -ae^{-ax} = 0$$



# MAT Final

$$\lim_{N \rightarrow \infty} \left(1 + \frac{R}{N}\right)^{NT}$$

$$\circ \ln \lim_{N \rightarrow \infty} \left(1 + \frac{R}{N}\right)^{NT}$$

$$\circ \lim_{N \rightarrow \infty} \ln \left(1 + \frac{R}{N}\right)^{NT}$$

$$\circ \lim_{N \rightarrow \infty} NT \ln \left(1 + \frac{R}{N}\right)$$

$$\circ \lim_{N \rightarrow \infty} \frac{\ln \left(1 + \frac{R}{N}\right)}{(N)^{-1}} = \frac{0}{0}$$

→ L'hopital

$$\circ \lim_{N \rightarrow \infty} \frac{\frac{1}{\left(1 + \frac{R}{N}\right)} - \frac{d}{dN} \left(1 + \frac{R}{N}\right)}{\frac{d}{dN} (N^{-1})}$$

$$\circ \lim_{N \rightarrow \infty} \frac{1}{\left(1 + \frac{R}{N}\right)} \cdot R(-N)$$

$$\frac{d}{dN} \cdot N^{-1} = -N^{-2}$$

No   
Hirotaki Tomooka



# PURPLE PARROTS

3.3

36)  $f(x) = x^2 e^{-4x}$  on a)  $[-2, 0]$  b)  $[0, 4]$

a) min =  $(0, 0)$

max = NONE

b) min  $(4, 1.8 \times 10^{-6})$   
max  $(0.5, 0.033)$

a)  $y_1 = x^2 e^{(-4x)}$

$x_{\min} = -2$

$x_{\max} = 0$

zoom fit

calculator work

Calc. 3: Min

Left -2

Right 0

Guess 0

$x = 0. \quad y = 0$

Repeat for Max.

3.4

$$y = x^3 - 3x^2 - 9x + 1$$

#4

$$y' = 3x^2 - 6x - 9 = 0$$

$$x^2 - 2x - 3 = 0$$

$$(x-3)(x+1) = 0$$



$y'(0) = -9$   $\uparrow$   $\ominus$   
Decreasing  $(-1, 3)$   
Increasing  $(-\infty, -1) \cup (3, \infty)$

Abraham Sherman  
Timothy Lubwicz

Biochemists

12) 3.4  
Find the limits  $\lim_{x \rightarrow 0} \frac{\tan x - x}{x^3}$

$$\text{L'Hopital } \frac{\sec^2 x - 1}{3x^2} = \frac{0}{0}$$

$$\text{L'Hopital } \frac{2 \sec x \cdot \sec x \tan x}{6x} = \frac{0}{0}$$

$$\text{L'Hopital } \frac{2[\sec^4 x + 2 \tan^2 x \sec^2 x]}{6}$$

$$= \frac{2[1 + 2(0)]}{6}$$

$$= \frac{2}{6} = \frac{1}{3}$$