

①

Change \rightarrow
 \rightarrow Increase
 \rightarrow Decrease
 \rightarrow constant

Rates of Change
 \rightarrow Average \rightarrow Need 2 POINTS.
 \rightarrow Instantaneous \rightarrow AT 1 POINT.

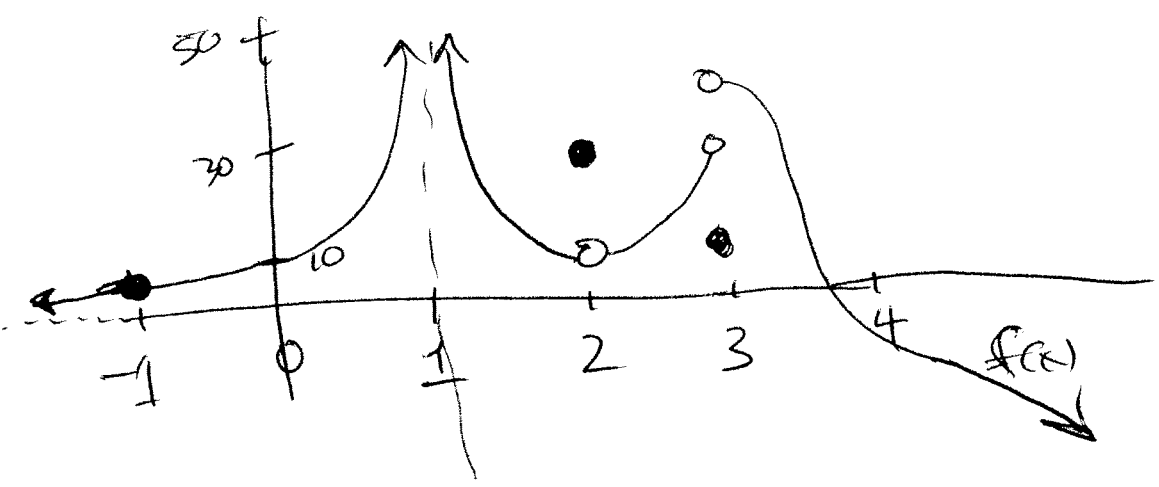
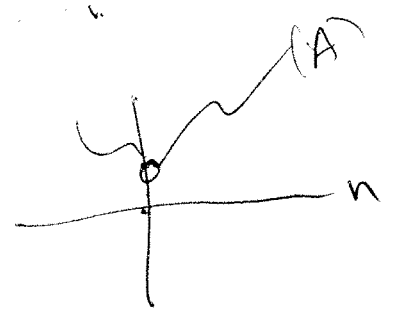


Limit

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{\cancel{h} - \cancel{h}} = \frac{\Delta Y}{\Delta X}$$

$$\lim_{h \rightarrow 0} \frac{h(A)}{h} = (A)$$

Picture



$$\lim_{x \rightarrow 0} f(x) = 10$$

$$f(0) = 10 \quad (2)$$

$$\lim_{x \rightarrow 1} f(x) = \infty$$

Doesn't matter
 $f(2) = 30$

$$\lim_{x \rightarrow 2} f(x) = 10$$

$$\lim_{x \rightarrow 3} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow 3^+} f(x) = 40$$

$$\lim_{x \rightarrow 3^-} f(x) = 30$$

$$\lim_{x \rightarrow -1^-} f(x) = 5$$

$$\lim_{x \rightarrow -\infty^+} f(x) = 0$$

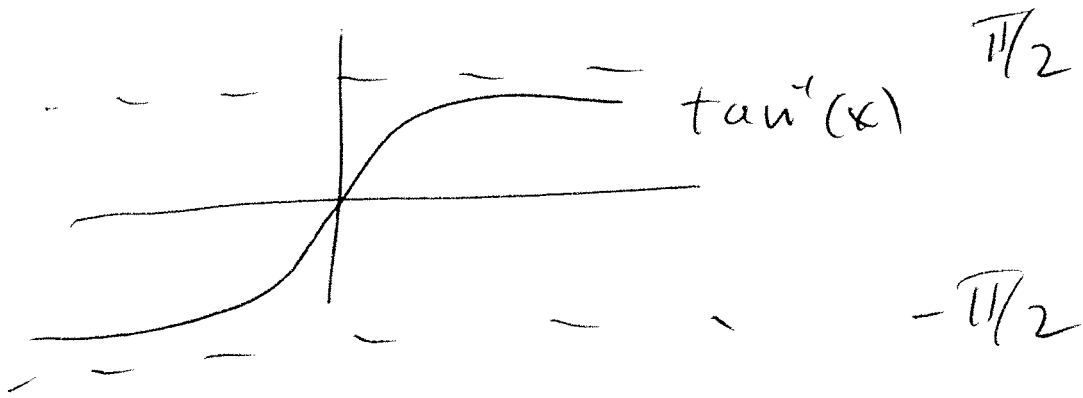
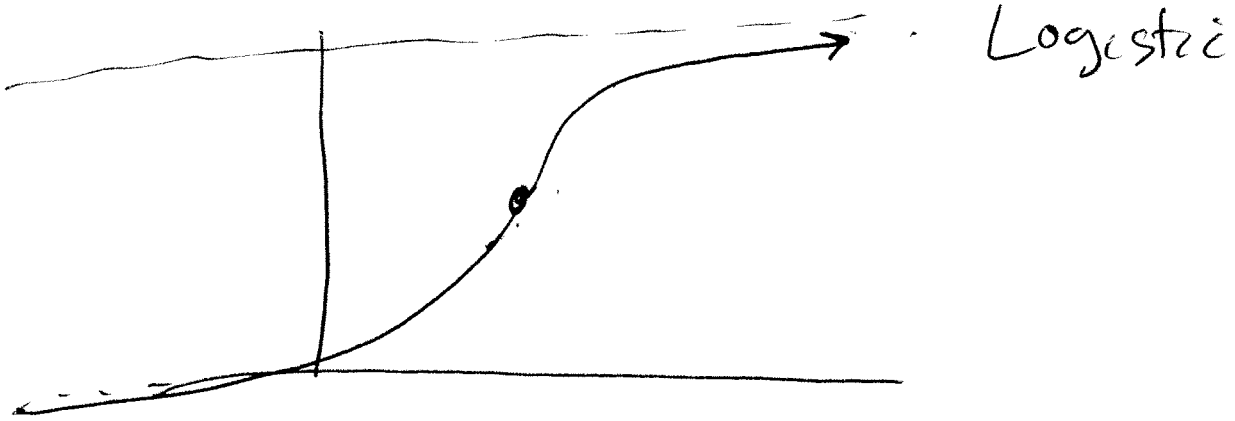
Left END
Behavior

Note: $\lim_{x \rightarrow -\infty^-} f(x) = \text{DNE}$

$$\lim_{x \rightarrow \infty} f(x) = -\infty$$

Right END
Behavior

(3)



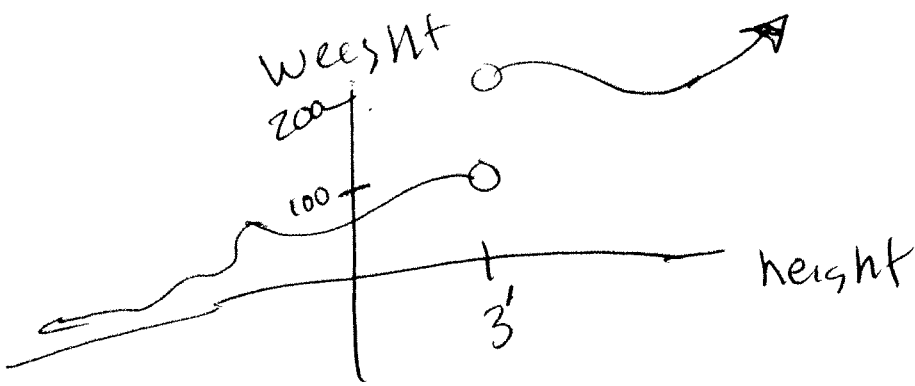
$$\frac{1}{\infty}$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} = 0$$

$$0 \cdot \infty$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} \cdot 3x = \lim_{x \rightarrow \infty} 3 = 3$$

$0 \cdot \infty$



Left
END

$$\lim_{\text{height} \rightarrow -\infty} r(x) = 0$$

Right
END

$$\lim_{\text{height} \rightarrow \infty} r(x) = \infty$$


As height goes to ∞ , weight goes to ∞
 " " " $-\infty$ " " " 0

$$\lim_{h \rightarrow 3^-} r(x)$$

$$\lim_{h \rightarrow 3^+} r(x)$$

~~As height goes to 3~~

As a "short" person grows to 3' we expect them to weight 100lb.
 As a "tall" person shrink to 3' we expect them to weight 200lb.

<p>GROUP NAME: <u>Mathletes</u></p> <p>Logo: </p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Kyle Inverso</u></p>
<p>Date: _____</p> <p>Topics: _____</p>	<p>Writer/Prep: <u>Aidan Callahan</u></p> <p>QC/Leader: <u>Logan Hockenbury</u></p>

Instructions:

x	y
1927	100
1937	92
1947	85
1957	72
1967	62
1977	51
1987	42

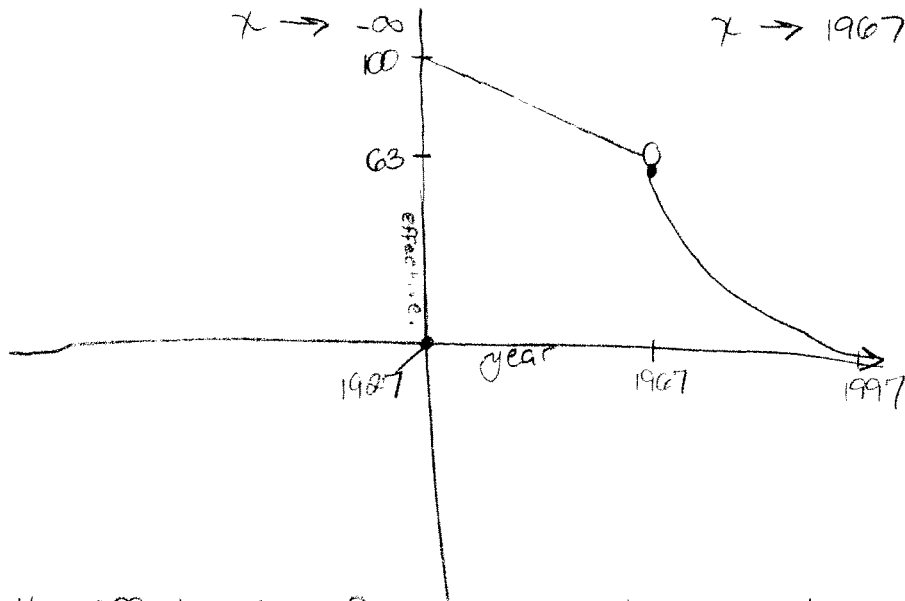
exponential regression
linear regression

$$\lim_{x \rightarrow \infty} r(x) = 0$$

$$\lim_{x \rightarrow -\infty} r(x) = 100$$

$$\lim_{x \rightarrow 1967^-} r(x) = 58$$


$$\lim_{x \rightarrow 1967^+} r(x) = 63$$



as time increases, the effectiveness of the bridge decreases to grade of 0.
as time decreases, the effectiveness of the bridge continues to increase above 100.

MATH!

GROUP NAME: IRISH BOMBS

Logo: 

Date: _____

Topics: _____

Student Names (First and Last) _____

Speaker/Presenter: Connor Kaysman

Writer/Prep: Bobby O'Connor

QC/Leader: The Real Bill Smith

Instructions:

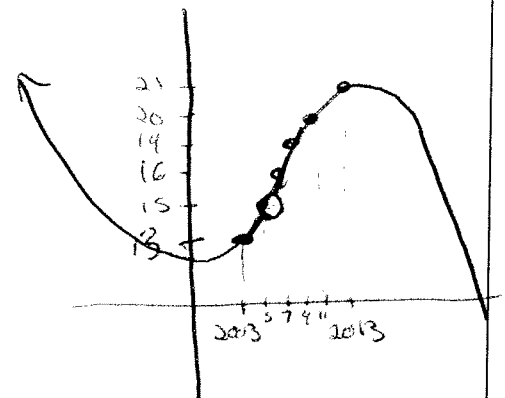
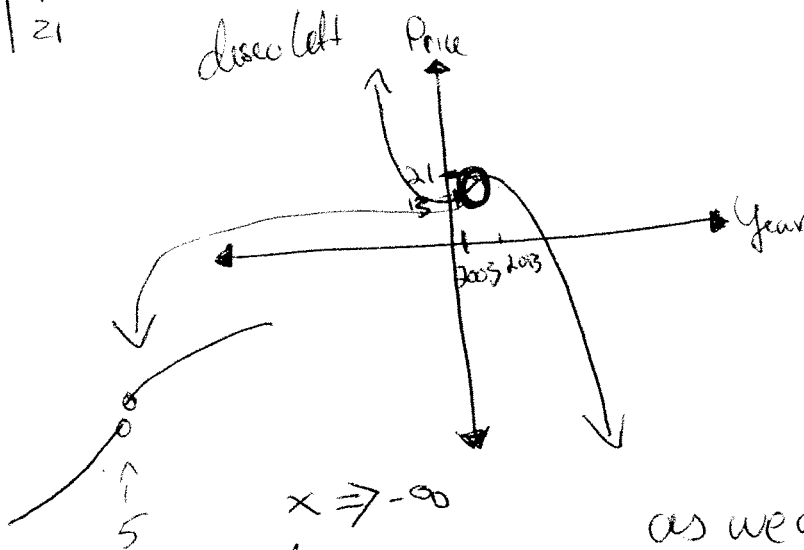
Limits

meow.

Year	Price
2003	13
2005	15
2007	16
2009	19
2011	20
2013	21

PBR PRICE OVER LAST 10 years

Limit ~~at~~ at 2005 Cubic & Quartic

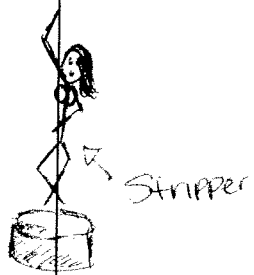


$x \Rightarrow -\infty$ as we go BACK TO THE FUTURE

left end behavior: as x approaches $-\infty$, the Price goes to ~~all~~ all the way up
 (in the immortal words of John Mellencamp) as "time goes on"

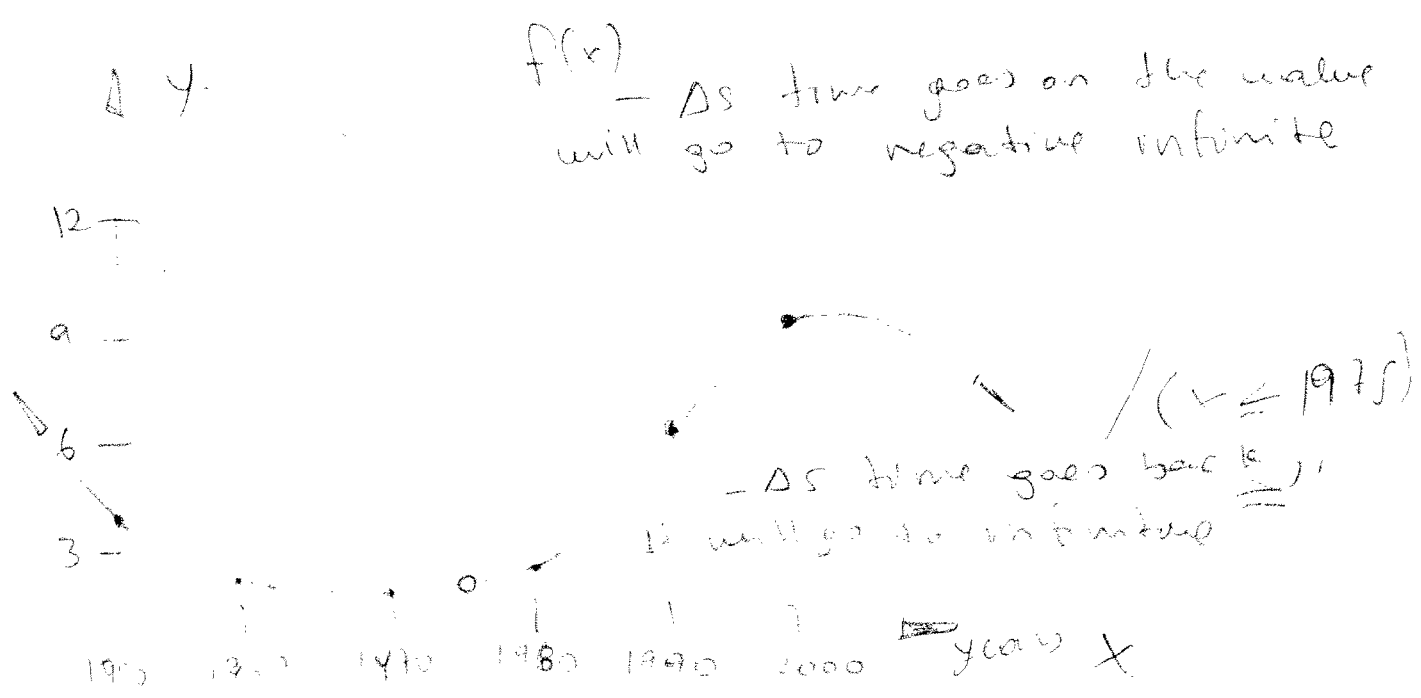
Right end behavior: as x approaches ∞ , the Price goes to ~~zero~~ zero
 $x \Rightarrow \infty$ less than nothing

as price \rightarrow 2005 from the future, you'll spend \$14.75
 as price \rightarrow 2005 from past, you'll spend \$14.63



GROUP NAME: <u>The Factors</u>	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Ryan Bigley</u>
Date: <u>9/4/13</u>	Writer/Prep: <u>Fiona Chang</u>
Topics: <u>Limits & End Behaviors</u>	QC/Leader: <u>Ethan Stewart</u>

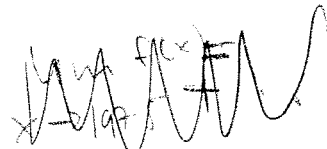
Instructions:



Time	Value
1950	2.5
1960	2.25
1970	1.85
1980	3.5
1990	6.7
2000	9.2

Right End Behavior $x \rightarrow d^+$

Left End Behavior $x \rightarrow d^-$



$$\lim_{x \rightarrow 1975^-} f(x) = 2.27$$

$$\lim_{x \rightarrow 1975^+} f(x) = 7.917$$

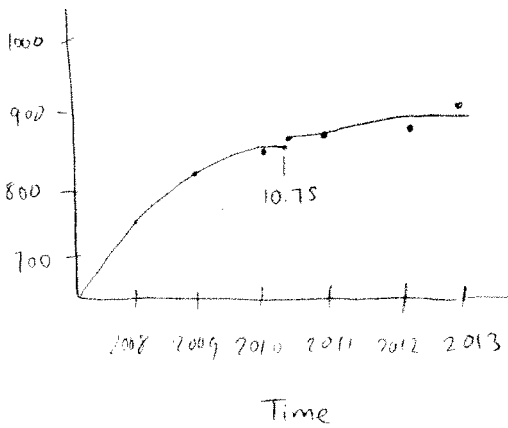
$$\lim_{x \rightarrow 1975^-} f(x) = 2.387499972 \$$$

$$\lim_{x \rightarrow 1975^+} f(x) = 2.38749997$$

GROUP NAME: <u>The Scientists</u>	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Dorin Cirotjan</u>
Date: <u>9/4/13</u>	Writer/Prep: <u>Hiersten Hendricksen</u>
Topics:	QC/Leader: <u>Nicole Perrier</u>

Instructions: $\lim_{x \rightarrow}$ $r(x)$

of documented
extinct species



$$\lim_{x \rightarrow -\infty} r(x) = -\infty$$

$$\lim_{x \rightarrow \infty} r(x) = \infty$$

$$\lim_{x \rightarrow 2010.75^+} r(x) = 869.45$$

$$\lim_{x \rightarrow 2010.75^-} r(x) = 856.22$$

As we travel back in time, the # of documented extinct species goes to 0

As we travel into the future, the # of documented extinct species approaches ∞

As we go back 10.75^+ [cubic regression] (Fall of year 2010)⁺, the # of documented species is 869.45

As we go forward 10.75^- (quadratic regression), the # of documented species is 856.22

GROUP NAME: <u>Wolf Pack</u>	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Jared S.</u>
Date: <u>9/4</u>	Writer/Prep: <u>DOMINIC C (DC)</u>
Topics: <u>Limits</u>	QC/Leader: <u>Quay</u>

Instructions:

YEAR	SPEED
1996	14
1998	28
2001	56
* 2003	5000
2006	10000

- * AS WE GO BACK TO THE BEGINNINGS OF TIME SPEED GOES TO $-\infty$
- * AS WE GO TO THE FUTURE SPEED GOES TO $+\infty$
- * AS WE GET CLOSE TO 2003 FROM THE PAST SPEED GOES TO 3444 kbs
- * AS WE GET CLOSE TO 2003 FROM THE FUTURE SPEED GOES TO 1318 kbs

GROUP NAME: Time Is Money



Logo:

Student Names (First and Last)

Speaker/Presenter: Angelika Mazurek

Writer/Prep: Shivam Singh (Shiv)

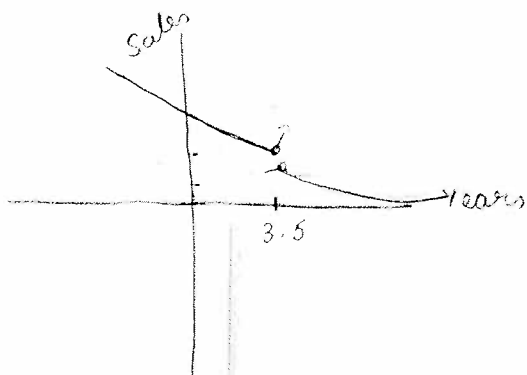
QC/Leader: Eugenio Pelaez

Date: 09/04/13

Topics:

Instructions:

LIMITS



Left
END $\lim_{\text{Years} \rightarrow -\infty} r(x) = \infty$

Right
END $\lim_{\text{Years} \rightarrow \infty} r(x) = 0.$

As the time goes on to ∞ the price goes to 0.

As the time goes back to $-\infty$ the price goes to ∞ (increases)

$\lim_{\text{Years} \rightarrow 3.5^-} r(x) = 394.05$

$\lim_{\text{Years} \rightarrow 3.5^+} r(x) = 349.5$

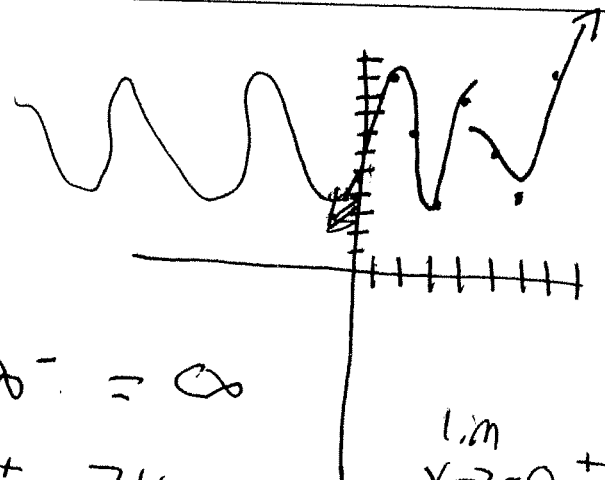
As the ^{time} goes back to 3.5^- we expect the price to be \$394.05 (Rise)

As the time goes on to 3.5 we expect the price to be \$349.5 (fall)

GROUP NAME: apples 2 apples	Student Names (First and Last)
Logo:	Speaker/Presenter: Steve H
Date: 9/04/13	Writer/Prep: Thomas y
Topics:	QC/Leader: Anna S

Instructions: Find limits approaching break & H asymptote

day	sleep
1	10
2	7
3	4
4	9
5	6.5
6	4.5
7	11



$$\lim_{x \rightarrow \infty^-} = \infty$$

$$\lim_{x \rightarrow 4^+} = 7.47$$

$$\lim_{x \rightarrow 4^-} = 10.03$$

$$\lim_{x \rightarrow -\infty^+} \text{DNE}$$

as we go further into the future sleep approaches infinity

as we approach day 4 from the left sleep is 10.03

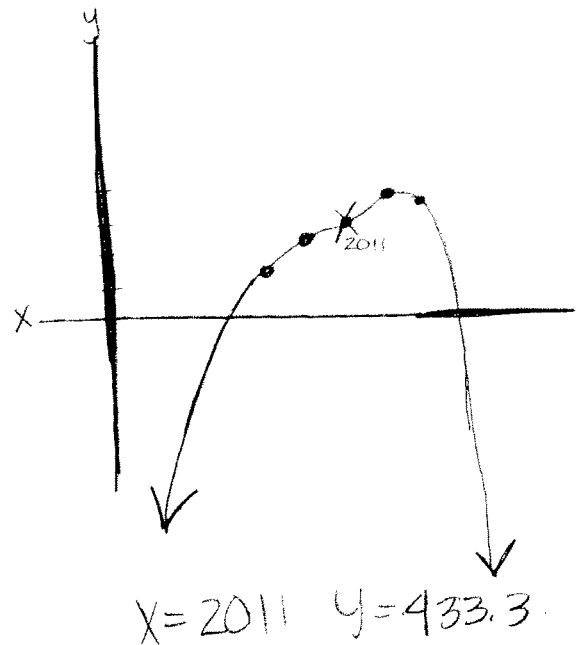
approaching day 4 from the right sleep is 7.47

GROUP NAME: CSC	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Cornel Douglas</u>
Date: <u>09/04/13</u>	Writer/Prep: <u>COURTNEY GRUBB</u>
Topics:	QC/Leader: <u>Stephen Smith</u>

Instructions:

APPLE STOCK PRICES

YR.	\$ PRICE
09	211.98
10	336.12
	405.00
12	532.11
13	501.02



as x approaches ∞ $f(x) = -\infty$

as x approaches $-\infty$ $f(x) = -\infty$

> as the years go by the stock decreases to nothing!

as the years approach to 2011 the stock will amount to nothing