

B.A is B.S

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$$4/6. f(x) = \frac{x^2}{(x-2)^2} \quad \frac{x^2}{x^2-4x+4}$$

a) horizontal and vertical

$$\frac{x^2}{x^2-4x+4} = \frac{\infty}{0} = 0 \quad \text{horizontal} = 1$$
$$x=2 \quad (2-2)=0 \quad \text{vertical} = 2$$

b) When does it increase/decrease

$$\frac{dx}{dy} f'(x) = \frac{2x}{2(x-2)(1)} = \frac{x}{2x-2} = \frac{-1}{2-1} = \frac{-1}{-6} = \frac{1}{6}$$

$$\leftarrow \begin{array}{cccc} + & + & - & + \end{array} \rightarrow \quad \frac{0}{0-4} = 0 \quad \frac{1}{-2} = \frac{1}{-1} = -1$$

c) local max/min

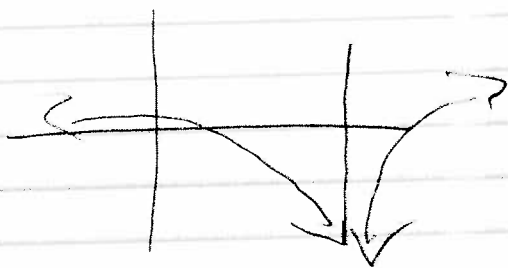
$$\frac{3}{6-4} \quad f(x) = \frac{x^2}{(x-2)^2} = \frac{2x}{x^2-2} \quad f'(x) = 0$$
$$x=0$$

$$(x-2)^3 = 0 \quad \text{local min} = 0$$
$$\text{local max DNE}$$

d) intervals of concavity and the inflection points

$$f(x) = \frac{x^2}{(x-2)^3}$$
$$f''(x) = \frac{6}{(x-2)^3}$$

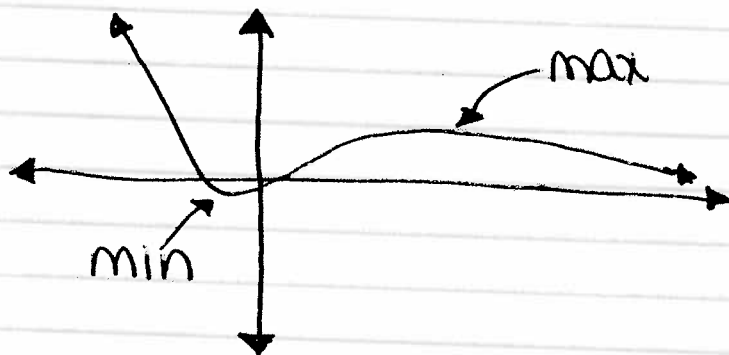
e) information from parts (a)-(d) to sketch



~~HW~~  
56

The New Group

$$f(x) = x^2 e^{-x}$$



Rough estimate. minimum  $-.053$   
Rough estimate maximum  $2.02$

$$f'(x) = 2x e^{-x} + x^2 e^{-x}$$

$$f'(x) = 2x e^{-x} + x^2 e^{-x}$$

$$f'(x) = e^{-x} (2x + x^2) = 0$$

$$\begin{aligned} \min \quad & x e^{-x} (2 - x) = 0 \\ & x = 0 \qquad 2 - x = 0 \\ & \qquad \qquad \qquad x = 2 \quad \text{max} \end{aligned}$$

4.3

# 58

TEAM: C.A.M.

$$f(x) = x^3 (x-2)^4$$

$$\begin{aligned} a) f'(x) &= 3x^2 (x-2)^4 + x^3 \cdot 4(x-2)^3 \\ &= x^2 (x-2)^3 [3(x-2) + 4x] \\ &= x^2 (x-2)^3 [3x-6+4x] \\ &= x^2 (x-2)^3 (7x-6) \end{aligned}$$

$$\begin{aligned} f'(x) = 0 \quad x^2 = 0 \quad x = 0 \\ (x-2)^3 = 0 \quad x = 2 \\ 7x-6 = 0 \quad x = 6/7 \end{aligned}$$

$$\begin{aligned} b) f'(x) &= x^2 (x-2)^3 (7x-6) \\ f''(x) &= 2x (x-2)^3 (7x-6) + x^2 \cdot 3(x-2)^2 (7x-6) + x^2 (x-2)^3 + \\ f''(x) &= x(x-2)^2 [2(x-2)(7x-6) + 3x(7x-6) + x(x-2)^2] \end{aligned}$$

$$f''(x) = x(x-2)^2 [14x^2 - 2x - 12x + 12 + 21x^2 - 18x + 7x^2 - 14x]$$

$$f''(x) = x(x-2)^2 [4x^2 + 72x + 12]$$

$$\begin{array}{cc} \downarrow & \downarrow \\ 0 & 0 \end{array}$$

Quadratic Formula

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-72 \pm \sqrt{3168}}{84}$$

$$= \frac{-72 \pm \sqrt{(72)^2 - 4(42)(12)}}{2(42)} = \frac{-72 \pm 56.28}{84}$$

$$= \frac{-72 \pm \sqrt{5184 - 2016}}{84} = \frac{-72 + 56.28}{84} = -0.187$$

$$\frac{-72 - 56.28}{84} = -1.527$$

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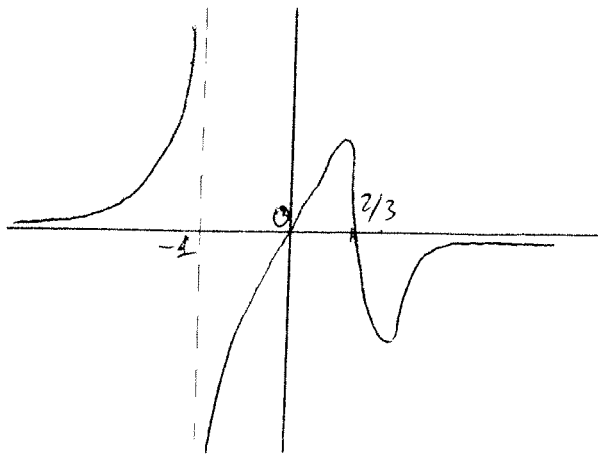
## FR3CH

4.3 # 60:

Estimate intervals of concavity of

$$f(x) = \frac{x^2 \tan^{-1} x}{1 + x^3}$$

Use calculator we have the graph of  $f''(x)$  below



Based on the graph we can estimate that:

$f(x)$  is concave up when  $x < -1$  since  $f''(x) > 0$

$f(x)$  is concave down when  $-1 < x < 2/3$  since  $f''(x) < 0$

$f(x)$  is concave up when  $0 < x < 2/3$  since  $f''(x) > 0$

$f(x)$  is concave down when  $x > 2/3$  since  $f''(x) < 0$

#62

1. 3000 = 2000 + 1000

a)  $f'(3) = 3$

$f''(3) = -$

Getting hotter

, Not going to stop

b)  $f'(3) = 2$

$f''(3) = -4$

Getting hotter, then cooling down / level OFF

c)  $f'(3) = -2$

,  $f''(3) = 4$

Getting cooler, then getting hotter

d)  $f'(3) = -2$

,  $f''(3) = -4$

Getting cooler, then getting cooler

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